MODELS OF POST-MIOCENE DEFORMATION OF THE ARABIAN PLATE

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Abstract. We investigate the deformation of the Arabian plate along a profile which extends from the Red Sea in the southwest to the Zagros in the northeast. The post-Miocene tectonic pattern of this region includes continuing uplift, volcanism, and extensional faulting at the western margin adjacent to the Red Sea; subsidence, folding, and thrusting at the eastern margin near the Zagros; and lack of major active tectonism in the interior. Thus, the near-surface state of horizontal deviatoric stress changes from extensional to compressional over a broad region of small tectonic stress. We derive models that can explain the observed distributions of stress and vertical displacement. The stress distribution within the plate is derived from the static equilibrium of the lithostatic load, deviatoric tectonic stresses, and shear stresses along the base of the lithosphere. The vertical motions are derived from nonuniform vertical deviatoric stresses at the base of the lithosphere. The models indicate that the post-Miocene deformation occurs by the combined effects of lateral density variations within the mantle part of the plate, ridge push at the Red Sea, and convective shear stress at the plate base. Density variations of 3.5% or less within the mantle part of the lithosphere induce a large portion of the tectonic stresses required for the observed deformation pattern in Arabia. The mean horizontal tensile tectonic stress in the lithosphere at the Red Sea cannot exceed 12.5 MPa for reasonable water depth in the Red Sea. The basal shear stress under Arabia must be directed toward the Zagros, and it ranges from 1 to 2 MPa. By modeling Arabia as a uniform viscous plate undergoing large-scale bending, we find that the tectonic stresses generated by the lithospheric density variations and basal shear stress are sufficient to upwar the Red Sea margins and downwar the Zagros zone. A lithosphere viscosity of 5 x 10^24 Pa s gives uplift of the Red Sea region at a rate of about 0.1 mm/yr.

INTRODUCTION

The central part of the Arabian plate, from the Rub-el Khali in the south to the Syrian desert in the north, is a 1500- to 1800-km-wide region that extends from the Red Sea in the southwest to the Zagros in the northeast. This region displays relatively simple
post-Miocene to Recent tectonic and structural patterns: uplift, volcanism, and extensional faulting characterize the western margin adjacent to the Red Sea, while subsidence, folding, and thrusting typify the eastern margins near the Zagros (Figure 1). Recent seismic activity is concentrated along both these margins (Figure 1). In the interior, there is a lack of features indicative of any intense late Tertiary deformation as well as a lack of large earthquakes in the recorded seismic activity. Thus, along a line trending roughly E-NE across the Arabian peninsula, the near-surface state of hori-
zontal deviatoric stress changes from extensional to compressional over a broad region of small tectonic stress. In the present study we briefly describe the main tectonic features of Arabia and derive a model that can explain their origin and distribution.

TECTONIC SETTING

The Arabian peninsula consists of Precambrian basement rocks, the Arabian shield, that are exposed in the west and are covered by sedimentary formations in the east (Figure 1). The shield is composed of metamorphic and igneous rocks whose last major tectonothermal event was the Pan-African, some 850-550 m.y. ago [e.g., Belski, 1982]. The shallow marine and continental sedimentary rocks comprise two zones: (1) a broad homocline and a few open basins north-east of the shield, and (2) the Persian Gulf-Zagros region (Figure 1) [Powers et al., 1967]. The sedimentary rocks of early Tertiary age and older were deposited when Arabia was part of the African plate and the Persian Gulf-Zagros was the continental margin along the Tethys ocean [e.g., Dewey et al., 1973]. The remnant of the Tethys ocean closed at the end of this period when continental collision commenced. The Arabian plate split from the African plate in the middle Miocene with the opening of the Red Sea and the Gulf of Aden [Cochran, 1981]. The generally northward moving Arabian plate [e.g., Garfunkel, 1981] is presently bounded by the oceanic ridges of the Red Sea and the Gulf of Aden, the Dead Sea transform, the Owen fracture zone, the Anatolian fault, and the thrust and fold belt of the Zagros and Taurus mountains (Figure 1).

Tectonic Features Along the Red Sea

Volcanism and extensional faulting. Several volcanic fields of Oligocene to Recent age form a 300 km by 2500 km belt along and north of the Red Sea (Figure 1) [e.g., Brown, 1972; Baker et al., 1973; Bender, 1974]. In Arabia, dikes, tuffs, and lava flows cover an area of approximately 10^6 km^2; flows of the Trap series in Yemen are the oldest Tertiary volcanic unit [Brown, 1972]. Some investigators distinguish between the Arabian peninsula volcanic province and the Jordan-Syria province on the basis of petrographic and structural differences [e.g., Brenner, 1979]. In general, the volcanics of Miocene age and younger in both provinces are alkali-olivine basalts [Baker et al., 1973; Gass et al., 1973; Brenner, 1979], and they differ from the more heterogeneous compositions of volcanics from the Red Sea and its islands [Gass et al., 1973]. The volcanic activity has continued in pulses from late Oligocene to the present [Bender, 1968; Brown, 1972].

Distinct lineaments are associated with this volcanism. Particularly conspicuous are the lines of volcanic cones trending N-S on the flows covering the Arabian shield [Brown, 1972] and the NNW to NW lineaments of Jordan and Syria [e.g., Bender, 1968; Schulmann, 1981] (Figure 1). Another set of lineaments are the reverse magnetic anomalies that extend for more than 1500 km along the Red Sea [Brown, 1972]. These anomalies are associated with basalt dikes, up to 100 m thick, that are partly exposed in Arabia [Brown, 1972] and Sinai [Steinitz et al., 1978] (Figure 1). The volcanic lineaments most likely reflect long cracks in the crust which serve as conduits for the rising magma.

Bender [1974] describes two systems of numerous long normal faults with minor displacements in southeast Jordan: a NW set and a NNW set (Figure 1). The generally northward moving Arabian plate [e.g., Garfunkel, 1981] is presently bounded by the oceanic ridges of the Red Sea and the Gulf of Aden, the Dead Sea transform, the Owen fracture zone, the Anatolian fault, and the thrust and fold belt of the Zagros and Taurus mountains (Figure 1).
Fig. 2. Generalized cross section through Arabia. Location of section shown in Figure 1. Dots: epicenters of earthquakes shown in Figure 1 and projected to the section; dashed lines: inferred Moho (northeast half of the section).
Crustal structure and seismic velocities (km/s) in segment A-B are after Mooney et al. [1985].
long dikes, the lines of volcanic cones, and the strikes of normal faults [Nakamura, 1977]. These directions range from the common N-S and NNW trends in Arabia, to the dominant NNW trend in Jordan-Syria (there are also some instances of E-W directions). Thus, the late Tertiary to Recent tension axes are between E-W, in Arabia, and E-NE in Arabia and Jordan-Syria.

Uplift of the Red Sea margins. Brown [1970] suggested that the rise of the eastern margins of the Red Sea began in the late Oligocene or early Miocene, that the magnitude of the uplift increases northward along the Red Sea, and that differential uplift occurred among separate blocks. Gass [1970], on the other hand, suggested that domal uplift centered above Afar began about 70 Ma and ceased after the Eocene. He proposed another domal uplift along the Red Sea, centered above 22°N.

M. Gettings (private communication, 1986) showed that uplift of Arabia commenced as early as the Cretaceous. The early uplift, which is not related to the opening of the Red Sea, is not restricted to the margins of the Red Sea, and it occupies large portions of Arabia. M. Gettings (private communication, 1986) estimates that only 1-2 km of margin uplift in southwestern Arabia is related to the Red Sea spreading.

The rate of uplift has been determined by fission track analysis in Sinai [Kohn and Eyal, 1981] and Arabia (M. Gettings, private communication, 1986). Kohn and Eyal [1981] found that the uplift in Sinai began 26 m.y. ago and has continued ever since; their results simply uplift rates as high as 0.2 mm/yr. The fission track results of Gettings indicate uplift rates of 0.02 to 0.03 mm/yr for Jiddah to Yemen escarpment, whereas his analysis of altitudes of lava flows indicates rates as high as 0.07 mm/yr.

Paleostress pattern in the Sinai subplate. The tectonic paleostress field along the Dead Sea Rift, western Arabia, has been recently determined from small-scale structures by Eyal and Reches [1983]. Their results indicate that the prevailing extension since early Miocene is the E-NE to E-W direction (Figure 1). The spatial distribution of the small structures suggests that the paleostress orientation is relatively uniform over hundreds of kilometers although the magnitude of the deformation is more intense along the Dead Sea Rift.

The subsurface structure of the western side of Arabia has been revealed in a recent series of geophysical investigations. These investigations include seismic refraction, gravity, heat flow, and magnetic measurements along a 1000-km-long profile from the axial trough of the Red Sea to the proximity of Riyadh (Figures 1 and 2) [Mooney et al., 1985; Gettings et al., 1986]. The structure of the lithosphere and the densities of the crust and the mantle calculated in these studies are used in the present analysis to estimate model parameters and to evaluate the model predictions.

Tectonic Features Along the Persian Gulf-Zagros Zone: Subsidence, folding, and thrusting

The northeastern margin of the Arabian plate is characterized by subsidence, sedimentation, and contemporaneous folding that date back to the early Miocene [e.g., Dunnington, 1958; Kamen-Kaye, 1970; Hull and Warmen, 1970]. That these processes started even earlier is suggested by pre-Eocene sedimentary rocks which are up to 3.5 km thick in central Arabia and at least 7 km thick in the Persian Gulf-Zagros zone. The subsidence and folding are restricted to a belt about 300 km wide west of the Zagros (Figure 1). The dominant rock types are limestones, anhydrites, rock salt, marine shale, and continental clastics. Intense folding has occurred within the Zagros zone since the late Miocene and particularly during the Pliocene [e.g., Dunnington, 1958]. Hundreds of long folds trending NW have developed along the zone (Figure 1); their wavelengths range from 5 to 30 km, and their amplitudes may exceed 5 km. Since folding is contemporaneous with sedimentation, the thicknesses of late Tertiary sediments vary significantly between anticlines and synclines. For example, the structural difference between the anticlinal crest and the synclinal trough in the Kuh-e-Khami, southwestern Iran, may exceed 9 km over a horizontal distance of only 20 km [Hull and Warmen, 1970]. Dunnington [1958] has suggested that the sedimentary thicknesses in the synclines give rough estimates of the magnitude of
subidence of the folded region during the Tertiary.

This active folding is associated with thrusting distributed in the crust. Bird [1978], using earthquake focal mechanism solutions, showed that the thrusting prevails throughout the whole crust, in a belt almost 400 km wide and 40 km thick (see also Figure 1). Both the folding and the thrusting indicate horizontal compression normal to the Zagros, i.e., in the E-NE direction.

Tectonic Features in Central Arabia

Hancock et al. [1984] analyzed the tectonic deformation of central Arabia using joint sets and subdued but long normal faults. The aggregate displacement of the oldest Neogene sediments along Wadi Al Batin faults is only 10-15 m. Since these faults are the most active faults in central Arabia, we consider central Arabia as lacking major tectonic activity during the post-Miocene period.

MECHANISMS FOR THE DEFORMATION OF ARABIA

The main post-Miocene tectonic features of central Arabia include the following deformation belts, from W-SW toward E-NE: (1) uplifted margins of the Red Sea in tectonic tension, (2) a stable zone almost 1000 km wide lacking in prominent active tectonic features, and (3) the Zagros zone of tectonic compression and subsidence. Seismic activity is concentrated in the Red Sea and the Zagros (Figures 1 and 2). In this section we derive models that can explain these distributions of stress and displacement. We determine the stress distribution within the plate from the static equilibrium of lithostatic stresses, deviatoric tectonic stresses, and shear stresses along the base of the lithosphere. The lithostatic load varies horizontally due to differences in density and crustal thickness between the lithosphere in the Red Sea and the Zagros. In our models the horizontal density variations are the main source of deviatoric tectonic stress and deformation [Fleitout and Froidevaux, 1982]. Other models [e.g., McGarr, 1982] consider basal shear as the major source of stress variations.
and the density of the mantle part of the lithosphere varies. These density variations reflect the temperature differences between upwelling mantle under the Red Sea and old subducting mantle under the Zagros. The lithosphere in model A is assumed to be in isostatic equilibrium with compensation depth $H$ along the entire profile (Figure 3). In model B, a nonzero vertical deviatoric stress is specified at $z = H$.

Elevated mantle of density $\rho_R$ lies beneath the Red Sea (Figure 3). The crust of the Arabian plate has density $\rho_c$, and its thickness is $h(x)$; here $h(0) = h_0$, and $h(x) - h_0$, where $x = 0$ is the Red Sea and $x = t$ is the Zagros zone. Subcrustal lithosphere has density $\rho_L(x,z)$ ($z$ is depth); $\rho_L$ increases from the Red Sea to the Zagros as a consequence of the decrease in temperature with distance $x$ from the upwelling mantle at the Red Sea spreading center. The increase in $\rho_L(x,z)$ toward the Zagros offsets the increase in crustal thickness $h(x)$ so as to achieve a state of isostasy in model A and a state of approximate isostasy in model B.

Model Solutions

We derive the deviatoric tectonic stresses for several configurations and boundary stresses. We search for situations that best fit the observed tectonic pattern of Arabia: extension and compression within the lithosphere along the Red Sea and the Zagros, respectively. Further, we search for tectonic stresses with magnitudes between about 5 and 50 MPa at the Red Sea and the Zagros, in accordance with the intensive seismic activity in these regions [Bird, 1978] (Figures 1 and 2).

The tectonic stresses $\sigma_t$ are calculated by solving the equation of force balance

$$F_R + F_h(x) + \sigma_t H + \sigma_b x = 0 \tag{1}$$

The formulas of Table 1 are used to calculate the lithospheric density and the forces $F_R$ and $F_h$; parameter values are listed in Table 2 (mostly after Gettings et al. [1986] and Bird [1978]. All forces are defined positive to the right (Figure 3).

Model A: stress distribution with isostatic equilibrium. Figure 4a shows $\sigma_t$ versus distance from the Red Sea $x$ for basal shear stress $\sigma_b = 0, 1, 2$ MPa and for two equivalent ridge structures: a water column of 6250 m directly overlying the mantle, and a water column of 2500 m overlying a 6750-m-thick crust of sediments and basalt of density 2000 kg m$^{-3}$ and the mantle. In both configurations the density of the mantle is 3330 kg m$^{-3}$ to a depth of 120 km, and the ridge force $F_R$ is $2.23 \times 10^{14}$ N m$^{-1}$. The density of the mantle part of the lithosphere, $\rho_L(x,z)$ (Figure 4b), is at most 3630 kg m$^{-3}$ or 3% larger than the density of the sublithospheric mantle.

The calculated deviatoric tectonic stresses are tensile along the Red Sea with a magnitude of about 12 MPa (Figure 4a). The tectonic stress at the Zagros depends on the magnitude of the basal shear stress: a basal shear stress smaller than 1 MPa is insufficient to
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Table 1. Analytic Formulas for Models A and B

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Ridge push force, $F_R$</strong></td>
<td></td>
</tr>
<tr>
<td>1. For direct water/mantle contact</td>
<td>( \frac{F_R}{\rho_R g H^2} = \left(1 - \frac{\rho_w}{\rho_R} \right) \left( \frac{1}{2} \frac{d^2}{H^2} - \frac{d}{H} \right) + \frac{1}{2} )</td>
</tr>
<tr>
<td>2. For water/oceanic crust/mantle sequence</td>
<td>( \frac{F_R}{\rho_R g H^2} = \left(1 - \frac{\rho_w}{\rho_R} \right) \left( \frac{1}{2} \frac{d^2}{H^2} - \frac{d}{H} \right) + \frac{1}{2} + \frac{\rho_b}{\rho_R} \left( \frac{1}{2} \frac{f^2 - d^2}{H^2} \right) + \frac{D-d}{H} )</td>
</tr>
<tr>
<td><strong>Vertical stress, Red Sea, $x = 0$, $z = H$</strong></td>
<td></td>
</tr>
<tr>
<td>1. For direct water/mantle contact</td>
<td>( \bar{P}_H = \frac{P_H}{\rho_R g H} = \frac{\rho_w}{\rho_R} \frac{d}{H} + \left(1 - \frac{d}{H} \right) )</td>
</tr>
<tr>
<td>2. For water/oceanic crust/mantle sequence</td>
<td>( \bar{P}_H = \frac{P_H}{\rho_R g H} = \frac{\rho_w}{\rho_R} \frac{d}{H} + \frac{\rho_b}{\rho_R} \frac{(D-d)}{H} + \left(1 - \frac{D}{H} \right) )</td>
</tr>
<tr>
<td><strong>Vertical stress, base of lithosphere $x \geq 0$, $z = H$</strong></td>
<td>( P(x,H) = P_H \left( 1 - m \left( 1 - \frac{x}{L} \right)^2 \right) )</td>
</tr>
<tr>
<td><strong>Lithosphere density</strong></td>
<td></td>
</tr>
<tr>
<td>1. For Model A,</td>
<td>( \rho_L = \rho_m \left[ 1 + \left( k_{zo} + k_{z \ell} \frac{x}{L} \right) \frac{H - z}{H - h(x)} \right] )</td>
</tr>
<tr>
<td>( x \geq 0, \quad H \geq z \geq h(x) )</td>
<td></td>
</tr>
<tr>
<td>( \ell \geq 0 )</td>
<td></td>
</tr>
<tr>
<td>where</td>
<td></td>
</tr>
<tr>
<td>( k_{zo} = \frac{2P_H(1-m)\frac{\rho_R}{\rho_m} - 2(\frac{\rho_c}{\rho_m} - 1) \frac{h_0}{H} - 2}{1 - \frac{h_0}{H}} )</td>
<td></td>
</tr>
<tr>
<td>( k_{z \ell} = \frac{2P_H(1-m + mn)\frac{\rho_R}{\rho_m} - 2(\frac{\rho_c}{\rho_m} - 1) \frac{h_L}{H} - 2}{1 - \frac{h_L}{H}} )</td>
<td></td>
</tr>
<tr>
<td>( h(x) = \frac{P_H (1-m \left( 1 - \frac{x}{L} \right)^2) \frac{\rho_R}{\rho_m} - \frac{1}{2} \left( k_{zo} + k_{z \ell} \frac{x}{L} \right)}{\frac{\rho_c}{\rho_m} - \frac{1}{2} \left( k_{zo} + k_{z \ell} \frac{x}{L} \right)} - 1 )</td>
<td></td>
</tr>
<tr>
<td>2. For Model B,</td>
<td>replace ( P_H ) by ( P_H \left( 1 + m \left( 1 - n \frac{x}{L} \right) \right) ), where ( m, n ) are constants (see text).</td>
</tr>
</tbody>
</table>
Table 1 (continued)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>Horizontal force due to lithostatic load, $F_h$</td>
<td>$\frac{P_h}{\rho_m g H^2} = \left(1 - \frac{\rho_c}{\rho_m}\right) \left(\frac{1}{2} \frac{h^2(x)}{H^2} - \frac{h(x)}{H}\right) + \frac{1}{2}$</td>
</tr>
<tr>
<td></td>
<td>$+ \left[k_z + k_x \frac{x}{H} \right] \left(\frac{1}{3} \frac{h(x)}{H^2} + \frac{h^2(x)}{H^2} - \frac{h^3(x)}{3H^4}\right)$</td>
</tr>
</tbody>
</table>

Notation and Definition

- $d$: depth of water in Red Sea for direct water/mantle contact
- $D$: depth of base of crust under Red Sea
- $h_0$: thickness of continental crust at the Red Sea
- $h_1$: thickness of continental crust at the Zagros
- $h(x)$: thickness of continental crust
- $H$: thickness of lithosphere
- $\rho_w$: density of water
- $\rho_m$: density of mantle under lithosphere
- $\rho_{mL}$: density of mantle part of the lithosphere
- $\rho_b$: density of mantle beneath the Red Sea
- $\rho_o$: density of oceanic crust
- $\rho_c$: density of continental crust

generate compressive stress at the Zagros, whereas $\sigma_b$ larger than 3 MPa reduces the width of the zone of high tensile stresses at the Red Sea to about 100-200 km and generates very high compression at the Zagros. A basal shear stress directed toward the Red Sea would generate tension in the Zagros and compression along the Red Sea.

Another solution is presented in Figure 5. Here, we consider the effect of a less dense mantle under the Red Sea [Getting et al., 1986]. In Figure 5, $\rho_R$ is 0.98 $\rho_m$ (or 3263 kg m$^{-3}$), and the two equivalent structures of the Red Sea are $d = 5.5$ km for the case with direct water/mantle contact and $d = 2.5$ km, $D = 9.25$ km, and $\rho_b = 2225$ kg m$^{-3}$ for the case with oceanic crust. The mantle part of the Arabian lithosphere in this case is less dense than the sublithospheric mantle (Figure 5b) with a minimum density of about 3220 kg m$^{-3}$. The tectonic stresses calculated for this configuration are similar to those in Figure 4a, but the magnitudes are smaller; maximum tension at the Red Sea is about 5.5 MPa (Figure 5a).

Model B: stress distribution with nonisostatic conditions. Vertical movements are evident in Arabia: uplift of the Red Sea margins and subsidence and sedimentation along the Zagros suture (see introduction). We regard these vertical motions as reflecting nonuniform vertical deviatoric stress $\sigma_v$ at the base of the lithosphere. The vertical deviatoric stress is modeled as

$$\sigma_v(x) = P_h \frac{m}{n} \left(1 - \frac{nx}{L}\right)$$

where $P_h$ is the lithostatic stress at $z = 120$ km under the ridge at the Red Sea (Table 1) and $m$ and $n$ are positive constants ($m < 1$); $\sigma_v$ is positive upward. Vertical deviatoric stress in shown plotted as a function of $x$ in Figure 6 for $m = 0.001$ and a few values of $n$.

There is a maximum upward vertical deviatoric stress at the margins of the Red Sea ($x = 0$) corresponding to the uplift there. The vertical stress at the Zagros depends on the magnitude of $n$; $\sigma_v(x = L)$ is downward for $n > 1$. Horizontal variations in vertical stresses at the base of the lithosphere are assumed to be associated with horizontal variations in lithosphere density as described in
TABLE 2. Parameter Values

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Symbol</th>
<th>Value or Range</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mantle density, kg m(^{-3})</td>
<td>(\rho_m)</td>
<td>3330</td>
<td></td>
</tr>
<tr>
<td>Below lithosphere</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>At Red Sea</td>
<td>(\rho_R)</td>
<td>(\leq 3330)</td>
<td>Gettings et al. [1986]</td>
</tr>
<tr>
<td>Crust density: Arabia, kg m(^{-3})</td>
<td>(\rho_c)</td>
<td>2900</td>
<td>Gettings et al. [1986]</td>
</tr>
<tr>
<td>Crust thickness, km</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>At Red Sea</td>
<td>(h_o)</td>
<td>38</td>
<td>Gettings et al. [1986]</td>
</tr>
<tr>
<td>At Zagros</td>
<td>(h_g)</td>
<td>46</td>
<td>Bird [1978]</td>
</tr>
<tr>
<td>&quot;Compensation&quot; depth, km</td>
<td>(H)</td>
<td>120</td>
<td></td>
</tr>
<tr>
<td>Water depth: Red Sea, km</td>
<td>(d)</td>
<td>2.5-7</td>
<td></td>
</tr>
<tr>
<td>Thickness of oceanic crust:</td>
<td>(D-d)</td>
<td>0-8</td>
<td></td>
</tr>
<tr>
<td>Red Sea, km</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 1. These density variations also determine the horizontal deviatoric stresses in the lithosphere according to the formulas of Table 1.

Horizontal deviatoric stresses and lithospheric densities are shown in Figures 7 and 8 for values of \(m\) and \(n\) chosen on the basis of bending calculations discussed later in the paper. In both figures, \(n = 2\) while \(m\) in Figure 7 is 0.0002 and in Figure 8 it is 0.0003. Other parameters in Figures 7 and 8 are as in Figures 4 and 5, respectively. The horizontal tectonic stresses and lithospheric densities are similar in the corresponding isostatic and nonisostatic models (compare Figures 4a with 7a and 5a with 8a). The small vertical deviatoric stresses in the nonisostatic models are directed upward at the Red Sea and downward at the Zagros with the same absolute magnitude 0.6 MPa at both locations (Figures 7a and 8a).

Summary

Models A and B lead to some general conclusions about deformation and stress in Arabia that are summarized here and in Table 3. Reasonable density variations within the Arabian lithosphere (Figures 4b, 5b, 7b, and 8b) generate tectonic stresses in agreement with the main tectonic zones (Figures 4a, 5a, 7a, and 8a). However, the mean tectonic stresses due to density variation alone are small, only a few megapascals. More realistic tectonic stresses require a 1- to 2-MPa basal shear stress directed toward the Zagros. The mean horizontal tensile tectonic stress in the lithosphere at the Red Sea cannot exceed about 12.5 MPa for a reasonable water depth in the Red Sea. Compressive stress at the Zagros depends on the magnitude of the basal shear stress. Following Bird [1978], we estimate that the deviatoric horizontal tectonic stress does not exceed 50 MPa. A vanishing basal shear stress would require an unreasonable water depth in the Red Sea (about 9 km), whereas a basal shear stress larger than 3 MPa would yield a compressive stress exceeding 50 MPa at the Zagros (Figures 4a, 5a, and 7a).

The stress transition across Arabia, from extension to compression, is gradual, and thus even the central part of the plate is subjected to small tectonic stresses of a few megapascals.
These stresses are insufficient to cause major tectonic deformation, and they are probably smaller than the local crustal strength.

Model for Bending of the Arabian Plate

The models discussed above deal only with the vertical average over the entire lithosphere of the horizontal tectonic stress; however, \( \sigma_b \) almost certainly varies with depth. Further, the models provide no information about the rheology of the lithosphere. In this section we address these aspects of the problem by analyzing the deformation of Arabia as the bending of a viscous plate.

The profile across Arabia, with uplifted Red Sea margins and the subsided Zagros zone, resembles a 1500-km-long plate which undergoes large-scale bending. We simulate this bending by the idealization in Figure 9: a plate with a stress-free upper surface, subjected to upward, downward, and horizontal displacement along its base. A standard plate bending solution [Reches and Johnson, 1978] can be applied if we regard the basal velocity as having a sinusoidal variation in the \( \xi \) or horizontal direction (Figure 9).

We take the tectonic stresses calculated above (Figures 4 to 8) and search for the bending solutions which are compatible with them.

We assume that the lithosphere can be considered as a viscous plate with mean viscosity \( \mu \) subjected to stresses and displacements along its boundaries. The present calculations are for plane strain conditions, with stress-free
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Fig. 6. Normalized vertical deviatoric stress $\sigma_v/P_H$ at the lithosphere base as a function of $x$ for $m = 0.001$ and several values of $n$. Values of $\sigma_v/P_H$ larger than zero indicate uplift while values smaller than zero indicate subsidence.

upper surface ($\sigma_{zz} = \sigma_{zz} = 0$ at $z = 0$) and specified velocities at the base of the lithosphere (Figure 9). We use the analysis of Reches and Johnson [1978, appendices I and II]; their formulas for velocities, deviatoric stresses, and boundary conditions are listed in Table 4. The vertical velocity at the base of the plate is $w_o \sin(\pi x/l)$, and the horizontal velocity is $-u_o \cos(\pi x/l)$.

A solution that generally fits the stresses calculated in models A and B is shown in Figure 10. The boundary velocities (Figure 10a), the horizontal deviatoric stress $\sigma_{zz}$ (Figure 10b), and the basal shear stràìs and basal vertical stress (Figure 10c) are shown for a plate 1500 km long and 120 km thick with a mean viscosity of $5 \times 10^{24}$ Pa s. The maximum vertical velocity along the base is $w_o = 0.1 \text{ mm yr}^{-1}$, and the maximum horizontal velocity at the base is $u_o = 0.002 \text{ mm yr}^{-1}$. The magnitudes of the viscosity and the basal velocities determine the magnitudes of the bending stresses, but they do not affect their spatial distribution (Table 4). Therefore, the plotted stresses can be adjusted to other uplift rates and viscosities by linear scaling.

Figure 10a shows how the velocities at the upper and lower surfaces of the plate vary with horizontal distance. Since the plate is relatively thin (aspect ratio = 12.5), the vertical velocity is essentially constant with depth, whereas the magnitude of the horizontal velocity increases upward by a small amount. Figure 10b shows how the deviatoric horizontal stresses $\sigma_{zz}$ at the top and bottom of the plate and the vertical mean of $\sigma_{zz}$ depend on distance from the Red Sea. The mean horizontal deviatoric stress ranges from 12 MPa tensile stress at the Red Sea to a compressive stress of the same magnitude at the Zagros. This mean horizontal stress is similar to the deviatoric tectonic stress $\sigma_b(x)$ in Figures 4, 7, and 8, for $\sigma_b$ of 1 to 2 MPa. Figure 10c shows variations with horizontal distance of the vertical

Fig. 7. Horizontal and vertical deviatoric stresses and lithosphere density for model B with the following parameter values $\rho_R = \rho_b = 3330 \text{ kg m}^{-3}$, $d = 2500 \text{ m}$, $D = 9250 \text{ m}$, $\rho_b = 2000 \text{ kg m}^{-3}$. There are small deviations from isostasy given by (2) with $m = 0.0002$ and $n = 2$. (a) Distribution of tectonic stresses. Dash-dot line: prescribed vertical, normal deviatoric stress $\sigma_v$ at the base of the lithosphere. Other lines are the average horizontal deviatoric stress $\sigma_b$ for three values of $\sigma_b$. (b) Density distribution in the Arabian lithosphere. Isodensity contours are labeled with the value of $\rho_b$ in kg m$^{-3}$. 

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A 20 I t t t t t t I t t ....

_  16 0 b -- 2 MPa .... -'"' -

o 12 .-" -

h8 ................ -

> 1 MPa -

r- 4  -

--

r- 'c. ......... // -

o o-4 ......... // -

'-. ....... // o b = 0

% -8

-12 i I i i I

300 600 goo 2oo

Distance from Red Sea (km)

e o

300 600 900 1200 1500

Distance from Red Sea (km)

Fig. 8. Similar to Figure 7 but with PR = 0.98 Pm and Pb = 2250 kg m⁻³.

deviatoric stress \( \sigma_{zz}(\xi,H) \) with maximum value of 0.6 MPa upward at the Red Sea, and \( \sigma_{zz}(\xi,H) \) with maximum magnitude of 3.2 MPa at the center of the plate. The mean shear stress along the base is 1.8 MPa toward the Zagros, in agreement with the values of \( \sigma_b \) inferred in the previous section (Figures 7 and 8).

The tectonic stresses determined by models A and B fit the stress field associated with bending of the Arabian plate. Density variations in the Arabian lithosphere generate tectonic stresses that are sufficient to bend the lithosphere along its entire 1500-km length between the Red Sea and the Zagros. For a lithosphere viscosity of \( 5 \times 10^{24} \text{ Pa s} \), these density variations produce uplift of the Red Sea region and subsidence of the Zagros region at rates of about 0.1 mm yr⁻¹. Figure 11 displays such a successful model for Arabia. The density distribution is from model B (Figure 8b), the vertical velocity distribution is from the bending analysis (Figure 10a), the horizontal normal stresses on lateral boundaries are from Figure 10b, and the basal stresses are from Figure 10c.

DISCUSSION

In this section we extend our previous discussion of the models and results to further assess how successful they are in explaining the major tectonic features of Arabia.

Density Variations Within the Models

The derived density distributions in the mantle part of the lithosphere (Figures 4b, 5b, 7b, and 8b) can be compared with the density profile across western Arabia (Figure 12) obtained by Mooney et al. [1985] and Gettings et al. [1986] from inversion of seismic refraction profiles and numerical analysis of gravity measurements. Mantle density variations in Figure 12 have the following major characteristics: (1) There is relatively light mantle just under the Red Sea (density of 3050 to 3070 kg m⁻³). (2) The uppermost mantle of the lithosphere, Moho to 60 km depth, is everywhere lighter than the underlying mantle, 60 to 120 km depth. (3) Mantle density increases toward the northeast; in the uppermost mantle the density increases from 3100 kg m⁻³ at the Red Sea to 3200 kg m⁻³ in central Arabia, and in the lowermost mantle the density increases from 3330 kg m⁻³ at the Red Sea to 3380 kg m⁻³ in central Arabia.

The density variations of Figure 12 are similar in sense, i.e., \( \rho_{m} \) increasing northeastward and downward, to the variations predicted by model A (Figure 5b) and model B (Figure 8b) with light mantle under the Red Sea. The magnitudes of the downward density increases in models A and B range from 30 to 100 kg m⁻³ (Figures 5b and 8b), whereas Figure 12 indicates a downward increase in \( \rho_{m} \) of 180 to 230 kg m⁻³. Our simple model has a crustal density that does not account for the crustal density variations with depth seen in Figure 12. These differences in crustal density must influence the comparison of subcrustal lithosphere density. Our model does include the increase in crustal thickness with distance from the Red Sea that is apparent in Figure 12.

The models of this paper predict mantle densities beneath Arabia in qualitative accord with those inferred from the seismic and gravity observations. It is significant then that
TABLE 3. Summary of Results (Models A, B, and Bending Model)

<table>
<thead>
<tr>
<th></th>
<th>Red Sea</th>
<th>Zagros</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Stresses, Velocities, and Viscosity</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Tectonic stresses (deviatoric, in MPa)</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Mean horizontal normal stress $\sigma_c$</td>
<td>-5.5 to -12.5</td>
<td>5.5 to 12.5</td>
</tr>
<tr>
<td>Maximum $\sigma_{xx}$ at surface ($z = 0$ km)</td>
<td>-28.3</td>
<td>28.3</td>
</tr>
<tr>
<td>Maximum $\sigma_{xx}$ at base ($z = 120$ km)</td>
<td>3.2</td>
<td>-3.2</td>
</tr>
<tr>
<td>Mean basal shear stress $\sigma_b$</td>
<td>1 to 2</td>
<td>1 to 2</td>
</tr>
<tr>
<td>Vertical basal normal stress $\sigma_v$</td>
<td>0.6</td>
<td>-0.6</td>
</tr>
<tr>
<td><strong>Velocities, mm yr$^{-1}$</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Maximum, vertical, at base</td>
<td>up 0.1</td>
<td>down 0.1</td>
</tr>
<tr>
<td>Maximum, horizontal ($x = 750$ km, $z = 120$ km)</td>
<td>0.002 westward</td>
<td></td>
</tr>
<tr>
<td>Mean lithosphere viscosity, Pa s</td>
<td>$5 \times 10^{24}$</td>
<td></td>
</tr>
</tbody>
</table>

these density variations can yield stresses that deform the Arabian lithosphere in a manner consistent with the observed tectonics and vertical displacements.

**Basal Shear Stress**

The present analysis indicates that shear stress directed toward the Zagros must exist at the lithosphere base; its magnitude is about 1 to 2 MPa (Figures 4a, 5a, 7a, and 8a). A zero basal shear

![Fig. 9. Bending model for Arabia showing basal velocities, $w_b \sin(\pi \xi / \xi)$ and $u_b \cos(\pi \xi / \xi)$, the stress-free upper surface, and the horizontal deviatoric normal stress $\sigma_{xx}$ along the lateral boundaries.](image)

is quantitatively unacceptable according to our model. For example, the solution in Figure 5a for zero basal shear implies that the horizontal tectonic stresses are about 1 MPa for the Zagros zone and about -5.5 MPa for the Red Sea. While the -5.5 MPa tensile stresses may be sufficient for extensional tectonic deformation, a compressive stress of 1 MPa at the Zagros is far below the expected few tens of megapascals in the Zagros [Bird, 1978]. The direction of this shear stress is in agreement with that expected from a mantle convection cell with hot upwelling material under the Red Sea and cold downwelling material under the Zagros. The magnitude of the shear stress is in accord with other estimates of basal shear stresses. For example, the analysis of Richardson et al. [1979, Table 2] indicates basal shear stresses for large plates in the range of 0.1-0.5 MPa. However, the basal shear for small plates may be much larger. Richardson et al. [1979, Table 3] found a basal shear stress of 2.19 MPa for Arabia in one of their better fitting models (model 29).

Our model may also provide a crude
TABLE 4. Analytical Solution for Bending of a Viscous Plate Under Plane Strain Conditions

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>$u$</td>
<td>$\frac{\left[\left[A + B(lz + 1)\right] \exp(\lambda z) + \left[C + D(lz - 1)\right] \exp(-\lambda z)\right] \cos(\lambda \xi)}{\sin(\lambda \xi)}$</td>
</tr>
<tr>
<td>$w$</td>
<td>$\frac{\left[\left[A + B(lz - 1)\right] \exp(\lambda z) - \left[C + D(lz + 1)\right] \exp(-\lambda z)\right] \sin(\lambda \xi)}{\cos(\lambda \xi)}$</td>
</tr>
<tr>
<td>$\sigma_{zz}$</td>
<td>$-2\mu \lambda \left[\left[A + B(lz + 1)\right] \exp(\lambda z) + \left[C + D(lz - 1)\right] \exp(-\lambda z)\right] \sin(\lambda \xi)$</td>
</tr>
<tr>
<td>$\sigma_{\xi \xi}$</td>
<td>$2\mu \lambda \left[\left[A + B(lz - 1)\right] \exp(\lambda z) + \left[C + D(lz + 1)\right] \exp(-\lambda z)\right] \cos(\lambda \xi)$</td>
</tr>
<tr>
<td>$\sigma_{z \xi}$</td>
<td>$2\mu \lambda \left[\left[A + B(lz)\right] \exp(\lambda z) - \left[C + D(lz)\right] \exp(-\lambda z)\right] \cos(\lambda \xi)$</td>
</tr>
</tbody>
</table>

Boundary conditions

$z = 0$

$\sigma_{zz} = \sigma_{\xi \xi} = 0$

$u = u_0 \cos(\lambda \xi), w = w_0 \sin(\lambda \xi)$.

Solution:

$C = (u_0 - w_0) - 2D\lambda H \exp(-\lambda H) + \exp(-\lambda H)$

$B = \frac{(u_0 - w_0) - D[2\lambda H \exp(\lambda H) + \exp(-\lambda H) + \exp(-\lambda H)]}{2[\exp(\lambda H) + \exp(-\lambda H)]}$

$D = \frac{-(u_0 + w_0)\left[\exp(\lambda H) + \exp(-\lambda H) + 2\lambda H(u_0 - w_0)\exp(\lambda H)\right]}{[\exp(\lambda H) + \exp(-\lambda H)]^2 + 4\lambda^2 H^2}$

The solution is after Reches and Johnson [1978].

*Here $\lambda = \pi / \ell$ ($\ell$ = length of plate); $\mu$ is plate viscosity; and A, B, C, and D are constants.

estimate of the velocity of this convective flow. Let us assume that the Arabian lithosphere had a uniform mantle density before the opening of the Red Sea, and that the calculated lateral density variations are solely due to heating by mantle flowing horizontally away from the center of upwelling in the Red Sea. The density variations are apparent at a distance of at least 800 km northeast of the Red Sea (Figure 11), and they may well extend further (Figure 8b). Therefore, the estimate of the advective velocity is 40 mm yr$^{-1}$ for a 20-m.y.-old Red Sea. This velocity is at least three times larger than the spreading rate of the Red Sea [Joffe and Garfunkel, 1987].

Bending of Arabia

Are the parameters and assumptions of the bending analysis reasonable? The applied uplift rate of 0.1 mm yr$^{-1}$ (Figure 10) is based on Kohn and Eyal's [1981] determination for the Sinai Peninsula. M. Gettings (private communication, 1986), on the other hand, found uplift rates for Red Sea margins of Arabia in the range of 0.03 to 0.07 mm/yr. Thus, the bending calculations for 0.1 mm/yr should be regarded as an upper limit. Given 0.1 mm/yr as the uplift rate together with the assumption of a mean lithosphere viscosity of 5 x $10^{24}$ Pa s, the bending model yields deviatoric stresses in agreement with those deduced from the simple balance of forces. Not only is the value of $\mu$ for the lithosphere supported by the inferred sensible stresses, but a lithosphere viscosity of 5 x $10^{24}$ Pa s is representative of other attempts [Walcott, 1973] to infer this parameter. An uplift rate of 0.05 mm/yr implies
either a lithosphere viscosity of $10^{25}$ Pa s and the same stresses as those of Figure 10, or a lithosphere viscosity of $5 \times 10^{24}$ Pa s and stresses of half the magnitude of those in Figure 10.

The assumption of a constant Newtonian viscosity for the continental lithosphere is a simplification of a complex rheology in which different constitutive behaviors probably characterize the upper crust, lower crust, and mantle [Goetze and Evans, 1979; Brace and Kohlstedt, 1980]. Nevertheless, the bending analysis predicts stress variations with depth that are in qualitative accord with the expected stress distribution in a more realistic model lithosphere.

Figure 11 shows that at the base of the lithosphere at the Red Sea, $\sigma_{xx}(0,H)$ is compressive and only a few megapascals in magnitude; $\sigma_{xx}(0,0)$ is tensile and tens of megapascals in magnitude at the top of the lithosphere at the Red Sea. At the Zagros, there are also large stresses at the top of the lithosphere and smaller stresses at its base (Figure 11), although the roles of compression and tension are reversed. The occurrence of high stress magnitudes at the top of the lithosphere versus low stress magnitudes at its base is in agreement with the expected strength distribution of the "layered" continental lithosphere [Kirby, 1983]. In addition, horizontal compression at the lithosphere base at the Red Sea and horizontal extension at the lithosphere base at the Zagros are in accord with

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**Fig. 10.** Results of the plate bending analysis for viscosity $= 5 \times 10^{24}$ Pa s and $\omega_0 = 0.1 \text{ mm yr}^{-1}$. (a) Distribution of vertical velocity $w$ at the base and top of the lithosphere (solid curve), horizontal velocity $u$ at the top (dashed line) and base (dotted line). Positive vertical velocity is upward, and positive horizontal velocity is westward. (b) The horizontal deviatoric stress $\sigma_{xx}$ at the top of the lithosphere (dashed curve) and at the lithosphere base (dotted curve), and the vertically averaged $\sigma_{xx}$ (solid curve). Tensile stresses are negative. (c) Deviatoric stresses at the base of the lithosphere. Vertical stress $\sigma_{zz}$ (solid curve), shear stress $\tau_{xz}$ (dashed curve), and vertically averaged shear stress (dotted curve). Basal shear toward the Zagros is negative.

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**Fig. 11.** A successful model for Arabia according to the present analysis. Density distribution after Figure 8b; velocity distribution after bending analysis (Figure 10a, vertical motions are highly exaggerated) and horizontal normal stresses on lateral boundaries after Figure 10b, and basal stresses after Figure 10c.
the stresses expected in a mantle convective cell with upwelling at the Red Sea and downwelling at the Zagros.

SUMMARY AND CONCLUSIONS

The Arabian plate shows a consistent tectonic pattern since the Miocene: uplift, volcanism, and extensional tectonics along the Red Sea, and subsidence, folding, and thrusting along the Zagros (Figures 1 and 2). This post-Miocene deformation occurs by the combined effects of lateral density variations within the mantle part of the plate, ridge push at the Red Sea, and convective shear stress at the base of the plate.

The Arabian plate is modeled as a 120-km-thick lithosphere with a constant density crust that is 38 km thick at the Red Sea and 45 km thick at the Zagros. The mantle part of the lithosphere becomes thinner and progressively denser from the Red Sea toward the Zagros; the mantle lithosphere also becomes denser with depth (Figures 5b and 8b). We determine the density of the mantle lithosphere by assuming isostasy or small prescribed departures therefrom and find that the maximum density difference in the lithosphere is 3.5% (Figure 8b). This value is smaller than the 8.3% maximum density difference computed from gravity data (Figure 12) [Gettings et al., 1986]. Thus, the density variations derived in our model (Figures 5b and 8b) are in qualitative agreement with those deduced from seismic and gravity data.

For a reasonable value of the ridge push force of 2.23 x 10^{14} N m^{-1}, the lateral density variations within the Arabian lithosphere produce small extensional stresses at the Red Sea and small compressive stresses at the Zagros. The magnitude of the tectonic stress is increased by a basal shear stress acting toward the Zagros (Figures 5a and 8a). The solution presented in Figure 8 is consistent with all the observational constraints; it involves a vertical normal stress of maximum magnitude 0.6 MPa at the base of the lithosphere. The vertical stress agrees with the observed uplift and subsidence along the margins of the Arabian plate.

The deformation of Arabia has been analyzed as a plate bending problem with uplift in the Red Sea and subsidence at the Zagros (Figure 9). The mean stresses associated with bending of the Arabian plate with mean lithospheric viscosity of 5 x 10^{24} Pa s and maximum uplift rate of 0.1 mm yr^{-1} are in good agreement with the mean tectonic stresses due to the density variations in the lithosphere, the ridge push force, and the basal shear.

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