



Dynamic fracturing: field and experimental observations

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Received 28 January 2000; accepted 7 December 2000

Abstract

We analyzed a system of complex joints in thick dolomite layers that are exposed within the western margins of the Dead Sea basin. These joints display two dominant features: 'tree-like' branching and a gradual increase of density that leads to local fragmentation. The development of this joint system is investigated in laboratory experiments with samples of brittle/ductile layered composites. The samples were subjected to layer-parallel extension and displayed three styles of fracturing: planar fractures, known from previous tests; branching fractures and clustering fractures, observed here for the first time in layered composites. Based on fracture morphology, we deduced that the branching and clustering fractures in the experiments, and the tree-like, closely spaced joints in the field, propagated at dynamic, high-velocity growth rates. It is proposed that the morphological features described here could be used as field criteria to recognize dynamic rates of rock fracturing. © 2001 Elsevier Science Ltd. All rights reserved.

Keywords: Fractures; Rock mechanics; Joints; Dynamic; Experimental; Tensile

1. Introduction

Countless fractures appear in the earth's crust. Many of them grow unstably and at high velocities, as evidenced by earthquakes and rockbursts. However, there is no systematic method to deduce the growth velocity of a fracture from its appearance in the field. Engelder and Fischer (1996) stated that "Even though propagation velocity is so important in identifying the joint-driving mechanism, little is known about natural joint velocity". Knowing the growth velocity of fractures is also important for applied problems such as seismic hazard evaluation, rockburst risk and the evaluation of fracture density in layered rocks. Fast growth of fractures is termed 'dynamic fracturing', a process in which tensile fractures grow at velocities comparable with Rayleigh wave velocity of the host material (Freund, 1990; Ravi-Chandar, 1998; Fineberg and Marder, 1999). In this study, we propose field criteria for dynamic fracturing of rocks and relate these criteria to new experimental results reported here.

Estimating joint propagation velocity in the field is not a simple task. One may deduce from explosive experiments that rock fractures associated with catastrophic events, like earthquakes, impacts or rockbursts, are dynamic fractures. Another approach is based on the experimental observations that slow growing fractures are smooth and simple, whereas

dynamic ones are rough and complex (e.g. Bahat, 1991; Lawn, 1993; Sharon and Fineberg, 1996). Using this approach, some fractographic features associated are suspected as indicating fast propagation. For example, Wallner lines and velocity hackles could indicate high propagation velocity (Kulander et al., 1979, pp. 26–34).

The first part of the present analysis describes the detailed geometry of joints within an exposure of dolomite layers close to the Dead Sea basin. The second part presents a series of experiments with brittle–ductile layered samples that were subjected to extension, and in which new fracturing styles have been observed. Finally, we suggest that the studied field joints grew at dynamic velocities and discuss the relations between dynamic fracturing and joint density. One should note that the term 'joint' is used here for an extension fracture observed in the field, whereas the more general term 'fracture' is used for a tensile (or shear) fracture observed in laboratory experiments.

2. Dynamic fracturing and fracture morphology

During slow, quasi-static propagation of fractures, the input of mechanical energy, U_M , is sufficient only for generation of new surface area of the growing fracture,

$$U_M + U_S = 0$$

where U_S is the new surface energy. During fast, dynamic fracture propagation, the input of mechanical energy, U_M ,

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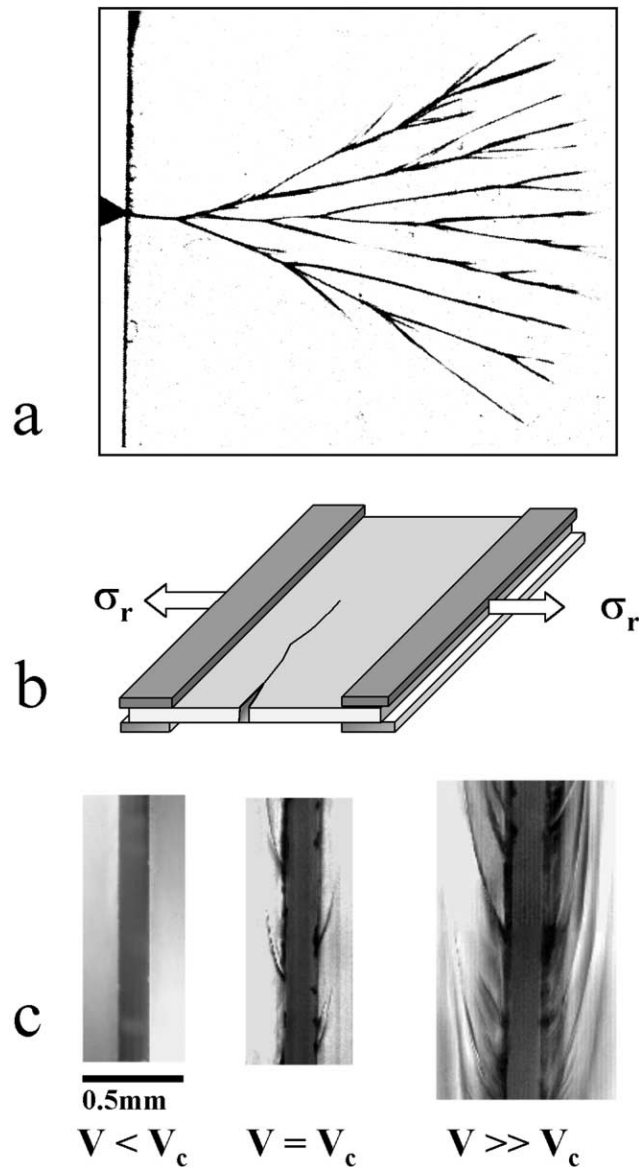


Fig. 1. (a) A branching system of a dynamic fracture in glass plate (Schardin, 1959); top view; the fracture propagated from left to right following a knife impact on the left side. (b) General morphology of a fracture growing in a $40 \times 40 \text{ cm}^2$ glass plate subjected to plate parallel quasi-static extension; σ_r is uniform tensile stress. (c) Close up view of fractures in the glass plate (map view); (left) smooth fractures that grow at a velocity below the critical velocity, $V < V_c$; (center) microbranches that develop when $V_c \approx 0.4V_R$; microbranches length and density increase with velocity (right); after Sharon and Fineberg (1996).

exceeds that necessary to form new surface area and the excess energy accelerates propagation to high velocities,

$$U_M + U_S + U_K = 0$$

where U_K is the kinetic energy of the dynamic fracture system. Theoretical analyses show that dynamic fractures could accelerate to a terminal velocity that equals the Rayleigh wave velocity of the host material (Freund, 1990). In most experiments, however, the terminal velocity

is smaller (Schardin, 1959; Ravi-Chandar and Knauss, 1984a,b).

A few types of geometric features are associated with dynamic fractures; note again that 'dynamic fracture' refers here to fractures growing at velocity V , which is comparable with Rayleigh wave velocity, V_R . The first type includes the mirror-mist-hackle zonation (Ravi-Chandar and Knauss, 1984b; Ravi-Chandar, 1998). The smooth, mirror zone forms when the fracture accelerates at a velocity that is less than a critical velocity. In the mist and hackle zones, the propagation velocity stabilizes at high value and the fracture surface becomes rough and irregular. The second geometric type includes the branching of dynamic fractures in brittle plates. This process generates large-scale branches that depart from the parent fracture, and propagate away from it (Fig. 1a) (Schardin, 1959; Lawn, 1993). The third type includes microbranches and minute surface roughness observed along dynamic fractures in plates of glass and PMMA (Fig. 1b and c) (Ravi-Chandar and Knauss, 1984b; Sharon and Fineberg, 1996, 1999). In these tests, the fractures are smooth when the propagation velocity, V , is smaller than a critical velocity, $V_c \approx 0.4V_R$; microbranches start to develop when $V \geq V_c$ (Fig. 1c) (Sharon and Fineberg, 1996). Further, the density of microbranches increases with velocity and the cumulative surface area of a fracture that grows at a terminal velocity of $V_T \approx 0.7V_R$ is six times the surface area of a planar fracture (Sharon and Fineberg, 1996).

In laboratory experiments, dynamic fractures develop under two loading conditions: very high strain rates ($\dot{\epsilon} > 10^3 \text{ sec}^{-1}$) generated by explosions or impacts (Dally, 1979; Ravi-Chandar and Knauss, 1982; Grady and Kipp, 1987); or quasi-static strain rates ($\dot{\epsilon} < 10^{-3} \text{ s}^{-1}$) associated, for example, with slow extension (Fineberg et al., 1992; Sharon and Fineberg, 1996). In the present paper, we analyze dynamic fractures that form under quasi-static strain-rates of $3.6 \times 10^{-5} \text{ s}^{-1}$ to $7 \times 10^{-3} \text{ s}^{-1}$, and develop tools to recognize dynamic fractures in the field.

3. Field observations

3.1. General

The fractures analyzed here are part of our regional study of faults and joints in the western margins of the Dead Sea basin (Sagy, 1999). The Dead Sea basin is a 100-km-long pull-apart between two left stepping segments of the Dead Sea transform (Fig. 2a) (Garfunkel, 1981; Reches, 1987). The 105 km of cumulative left-lateral slip along the transform began about 15 million years ago, and led to sediment accumulation in excess of 10 km (Garfunkel and Ben-Avraham, 1996). On its western side, the Dead Sea basin is bounded by a belt with many segmented normal faults in a zigzag pattern (Reches and Sagy, 1999; Sagy, 1999). This belt occupies a region that is more than 100 km long,

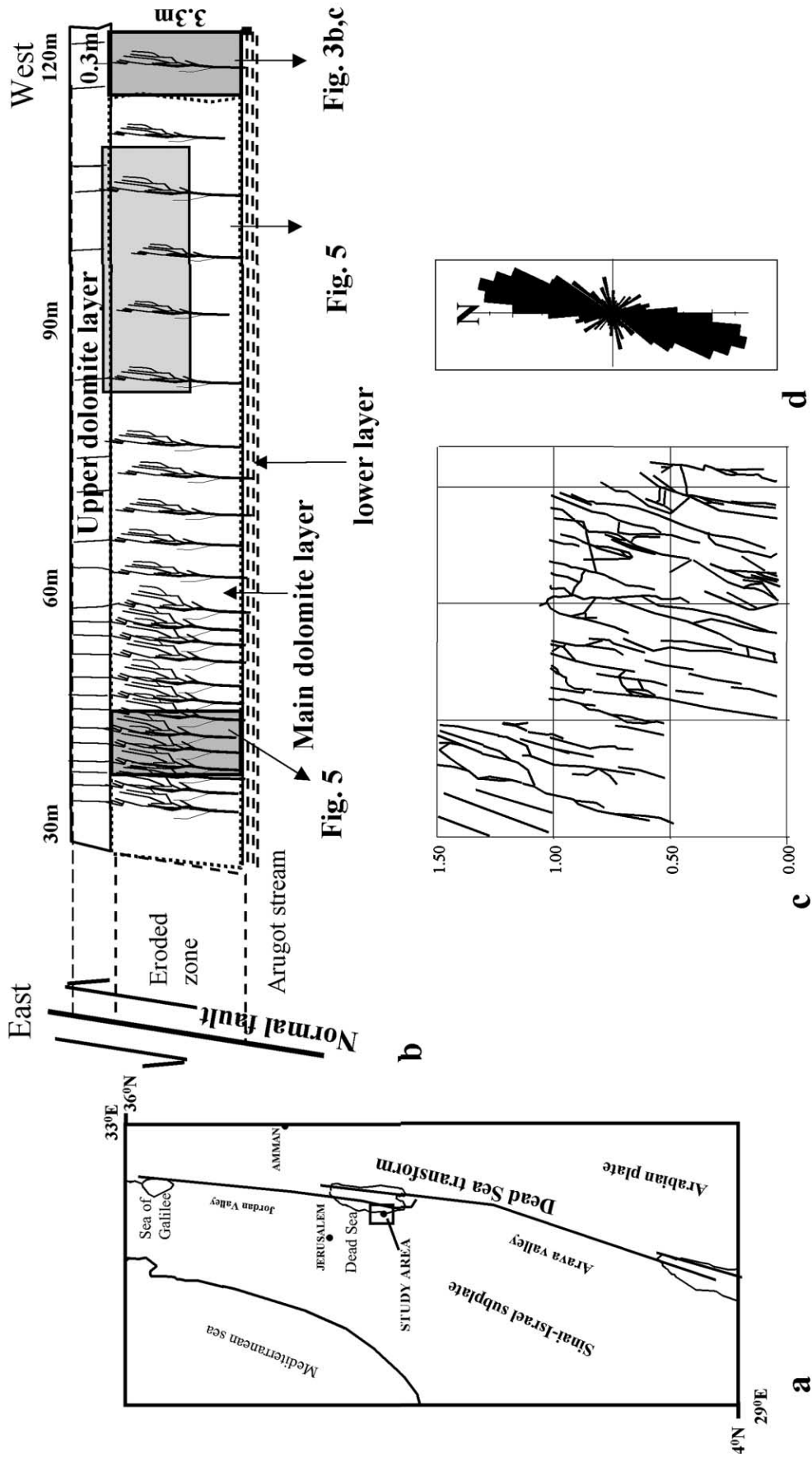
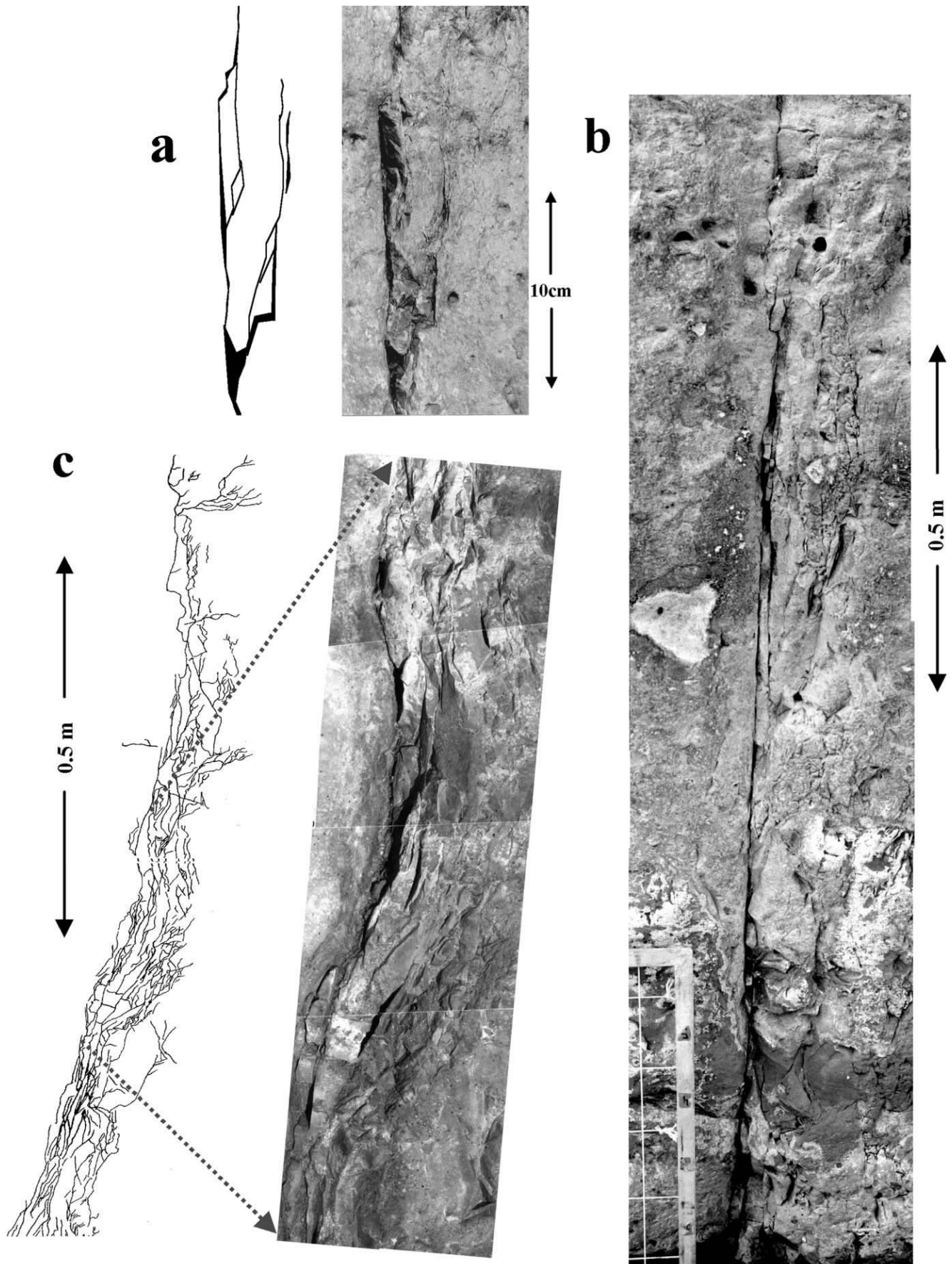


Fig. 2. (a) Location map of the study area in the Dead Sea basin. (b) Schematic cross-section of a sub-vertical wall in the Arugot outcrop, western margins of Dead Sea basin; shown: the main dolomite layer (3.3 m thick), tree-like joints, the eastern normal fault and the locations of the marked joints (shadowed rectangles); top scale indicates distance in meters from the eastern fault. (c) A joint map on top of the main dolomite layer at a distance of about 45 m west of the fault; mapping 1.75 m² at a 1:10 scale. (d) Rose diagram of joint strikes in the map shown in (c).



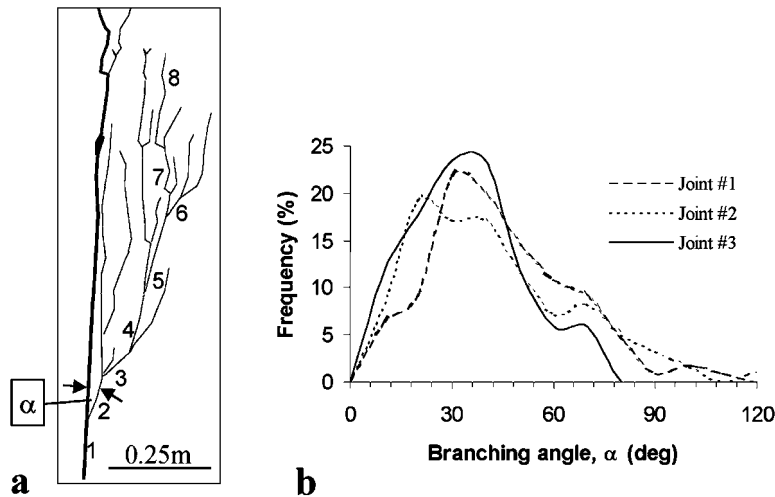


Fig. 4. (a) Branching along a single tree-like joint with eight marked offspring levels; heavy line indicates the main fracture; α marks the angle between the main fracture and branch level 2. (b) Histograms of branching angles α along three joints; joint #2 shown in Fig. 3c and joint #3 is the upper portion of Fig. 3b.

3–5 km wide and with cumulative vertical displacement of up to 10 km along its many faults. The faulting within the belt exposes a thick sequence of brittle carbonate rocks with networks of fractures and countless fragments. We studied in detail a highly complex joint system that is exposed within a 120-m-long outcrop in Arugot stream, central Dead Sea basin (Fig. 2a).

The Arugot outcrop includes sub-vertical walls that are 1.5–4.5 m in height, which form natural, vertical sections of the jointed layers. The analysis focuses on a 3.3-m-thick, flat lying layer of brittle, massive dolomite that is capped by a less competent dolomite layer, about 0.3-m-thick (Fig. 2b). To estimate the mechanical properties of these layers, we used the Schmidt hammer technique following the procedure of Katz et al. (2000). This procedure transforms elastic rebound values measured in the field into the Young modulus, uniaxial strength and density of rocks. The results for the 3.3-m-thick, massive dolomite layer indicated a Young modulus of 34 ± 6 GPa and a uniaxial strength of 109 ± 30 MPa. The overlying 0.3-m-thick dolomite layer is significantly less competent with a Young modulus of 12 ± 3 GPa and uniaxial strength of 34 ± 6 MPa.

We mapped the exposure of vertical section at a scale of 1:20, and selected portions at scales of 1:10 and 1:2; some individual joints were mapped at a 1:1 scale on enlarged photographs. Both layers are fractured by one set of sub-vertical joints that trends in a NNE–SSW direction (Fig. 2c and d); this set is one of the two dominating regional sets (Reches and Sagy, 1999; Sagy, 1999). The extensional nature of these joints is evident by the occurrence of ribs and hackles, and lack of shear displacements. This exposure

is bounded on its eastern side by a large normal fault that is one of the main boundary faults of the Dead Sea basin; its vertical displacement apparently exceeds hundreds of meters.

3.2. 'Tree-like' morphology of a single joint

An individual joint in the studied layer is a network of many short cracks arranged in a branching structure that is defined here as a 'tree-like' joint. In Fig. 3a, the main joint surface appears on the left side with one large secondary branch diverging to the right (lower part) and another, smaller secondary branch occurs about 7 cm above the first. Tertiary branches diverge from the secondary ones, and frequently, after a distance of 1–3 cm, the secondary and tertiary branches parallel the main surface. Some of the branches link again to the parent fracture (Fig. 3a).

The joint of Fig. 3a is relatively simple, whereas the common fractures in this exposure are significantly more complex, as shown in Fig. 3b and c. These joints include a main surface that is relatively long and which is composed of several quasi-planar segments linked to each other. The main surface becomes irregular and crooked in the upward direction and frequently the fracture terminates within the layer (Fig. 3b). The secondary branches diverge with a predominantly upward direction (Fig. 3c). The branching angles, α , (Fig. 4a) between the parent fractures and the branches were measured along three tree-like joints; the mean value is $43.0 \pm 22.5^\circ$ for the 298 measured angles (Fig. 4b). Most branching fractures are a few centimeters long but some extend up to a few decimeters from the parent fracture. Many of them curve to become parallel with the main fracture (Fig. 3).

Fig. 3. Tree-like joints in a dolomite layer (location in Fig. 2); note the upward branching, and parallelism of branches to the main fracture. (a) A relatively simple fracture shown by photograph (right) and map (left). (b) A large tree-like fracture with fairly smooth main fracture. (c) A complex, wide joint, photograph (right) and map (left); note width of more than 10 cm, and upward narrowing of the tree structure.

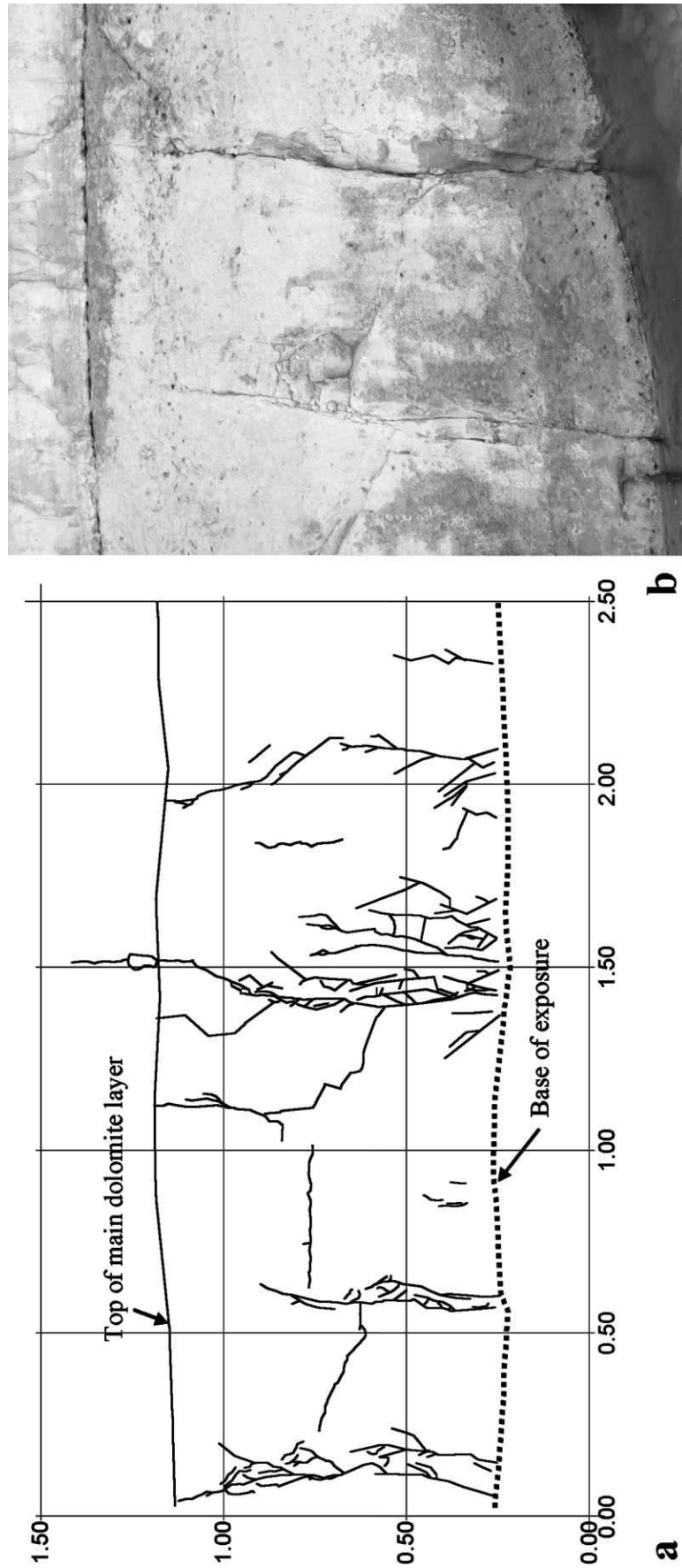


Fig. 5. Tree-like joints far away from the fault. (a) A cross-section view of several joints in the upper part of the main dolomite layer at a distance of ≈ 80 m west of the fault (location in Fig. 2). (b) Photo of two joints at a distance of ≈ 95 m west of the fault.

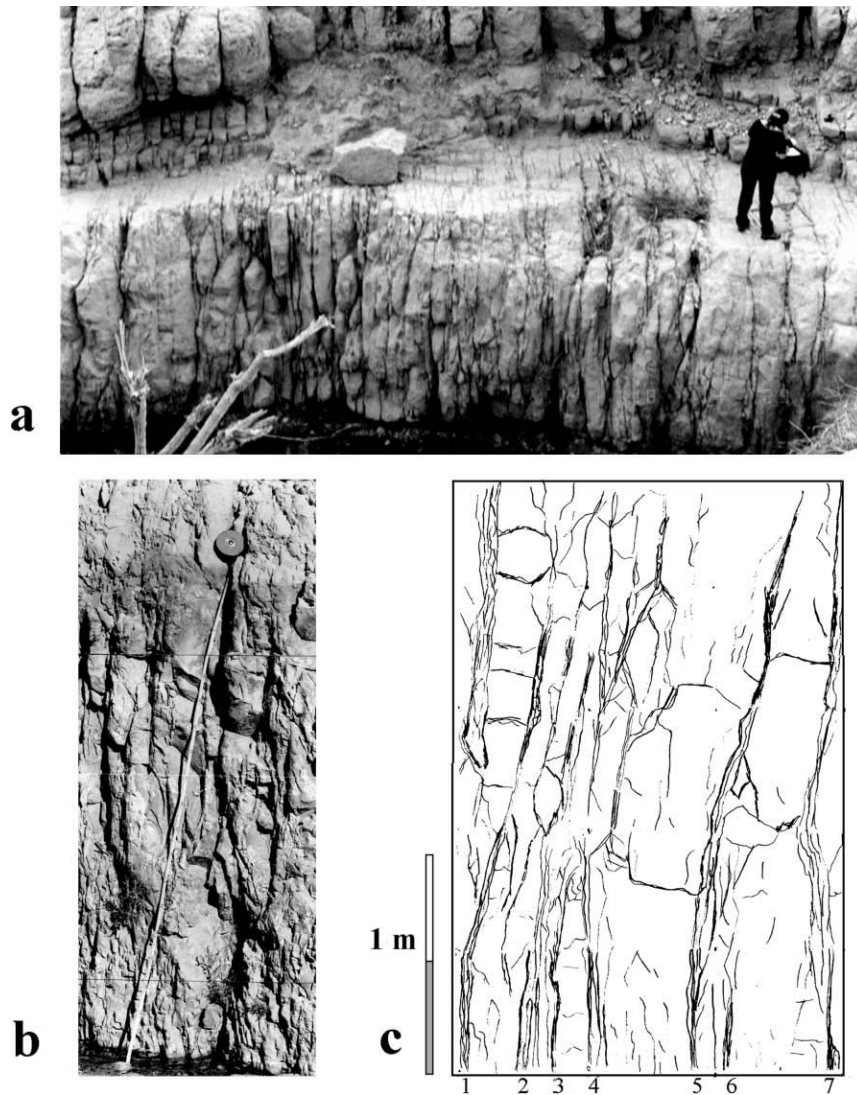


Fig. 6. High density of joints in the Arugot exposure (location in Fig. 2); general view (above) and close-ups below; note close spacing and cross-cutting relations of the fractures; e.g. in C one can recognize at least seven tree-like joints.

The tree-like joints display up to ten levels of branching (eight levels shown in Fig. 4a). This multiple branching generates a joint which is a wide zone of intense fracturing ranging in width from 1 to 15 cm (Figs. 3b and c and 4a). Local high density of the branches leads to total fragmentation of parts of the rock (Fig. 3c). We mapped, on a 1:1 scale, all branches associated with a few large tree-like fractures observed on the 2D-exposure wall. The maps show a cumulative fracture length of 9–14 m per meter of linear height of the main fracture; these results correspond to a surface-area of 9–14 m² per 1 m² of a planar fracture.

The abundance of branches is not constant even along a single joint. Branching intensity usually decreases upward along a typical joint, leading to a gradual upward narrowing of the tree-like joint (Fig. 3b and c). At a distance of ~100 m west of the fault, four out of five joints terminate within the layer and do not cross the layer top (Fig. 5). This

behavior changes dramatically eastward and at a distance of ~30 m from the fault all major joints cross the layer top (Fig. 6).

The occurrence of tree-like joints in the field is reported here for the first time. The main morphological features of the tree-like joints in Arugot are the following:

1. intense, multiple branching with up to 10 offspring levels starting from the main surface;
2. consistent upward direction of branching;
3. many of the branches tend to parallel the main surface;
4. branching angles vary significantly with average value of $43.0 \pm 22.5^\circ$;
5. development of 'wide', internally fragmented joints that are up to 15 cm in width;
6. the surface area associated with a wide tree-like joint is as high as one order of magnitude greater than the surface area of an equivalent planar joint.

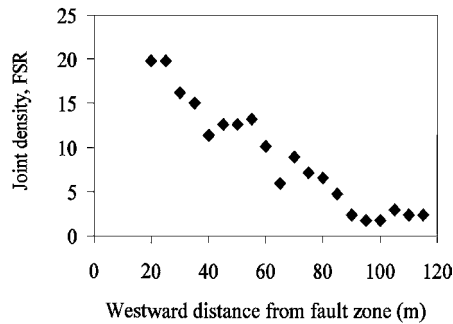


Fig. 7. Density of the tree-like large joints (height >2.0 m) measured in 5-m-long segments along the Arugat exposure; FSR values are plotted as a function of distance from the normal fault on the east.

3.3. Joint density

The distribution of tree-like joints varied in the studied exposure. At a distance of 90–120 m west of the fault, the joints were spaced at 1–1.5 m and the spacing was irregular (Figs. 2b and 5). Eastward, closer to the fault, the large joints became closely spaced with spacing of 0.2–0.3 m (Fig. 6c). The density of tree-like joints was calculated using the following procedure. First, the sub-vertical southern wall of the outcrop was mapped at a scale of 1:20 between 60 and 120 m west of the fault (location in Fig. 2b). Second, all tree-like joints higher than 1.5 m in the entire exposure were logged (the interval was 30–120 m west of the fault); 295 tree-like joints were counted here. Each tree-like joint was counted once and its associated branches were ignored; for example, two, four and seven joints were counted in Figs. 5b, 5a and 6c, respectively. Third, the mean spacing of these tree-like joints was calculated for 5-m-long segments. The calculated values were for joint-normal spacing after a correction for the difference between joint orientation and outcrop orientation. Finally, the density of the tree-like joints was calculated for these segments in the interval 30–120 m. The density parameter is a slightly modified version of FSR, the ‘Fracture-Spacing-Ratio’ of Gross (1993),

$$FSR = T/S$$

where T is the thickness of the mechanical host layer and S

is the mean joint spacing. Gross (1993) used median spacing for S to better represent a positively skewed spacing distribution. The present work deals with lateral variations of the joint density in one layer, and thus the mean spacing provides a suitable presentation for the intensity of jointing.

The joint density increases significantly toward the fault (Fig. 7). FSR is about two at a distance of 80–100 m west of the fault (Fig. 5), and it increases systematically to more than 20 at 30 m distance from the fault (Fig. 6). This increase is associated with several structural changes. Four out of five tree-like joints terminate within the layer at distance of ~ 100 m from the fault, whereas all tree-like joints cross the entire layer in the proximity of the fault (Fig. 6). Further, in the fault proximity, branches of neighboring tree-like joints coalesce with each other and the layer is totally fragmented (Fig. 6). The blocks between the fractures lose their continuity, large joints that cross the entire layer cannot always be distinguished from each other; for example, seven such large joints were labeled as 1–7 in Fig. 6c. The last 30 m of the dolomite layer closest to the fault were eroded, most likely due to intense fragmentation. Possible mechanisms for this high joint density are discussed later.

4. Experimental work

4.1. Experimental setup

We conducted a series of tests with layered composites to explore the mechanisms of high density jointing. Each sample includes three elongated layers. The upper and lower ones are ductile polycarbonate layers, and the central one is brittle epoxy (Fig. 8). Aluminum spacers were used as end-pieces to strengthen the gripping zone of the sample (Fig. 8). The polycarbonate layers are 3 mm in thickness, 200 mm in length and 30 mm in width, and the aluminum spacers are 1 mm thick and $30 \times 30 \text{ mm}^2$ (Fig. 8). The upper and lower polycarbonate layers were cemented to each other by the brittle epoxy with the aluminum spacers at the end zones. As a result, the 1-mm-thick central layer is divided into three parts: an epoxy part that is 140 mm in length and 30 mm in width, and two aluminum spacers that are $30 \times 30 \text{ mm}^2$ (Fig. 8). Material properties are listed in

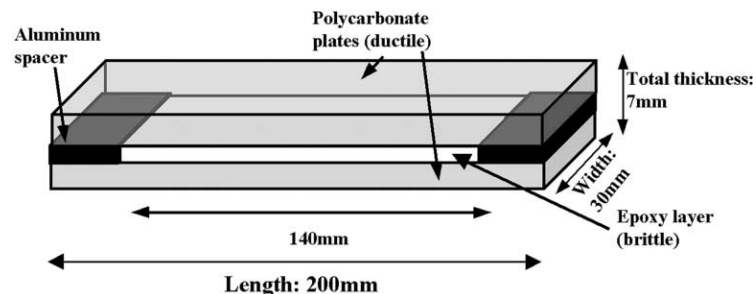


Fig. 8. Geometry of the samples used in the present extension experiments (see text).

Table 1

Mechanical properties of the components of the composite samples. Measurements were conducted under strain rates of $1\text{--}2 \times 10^{-3} \text{ s}^{-1}$

	Young modulus (MPa)	Tensile strength (MPa)	Tensile strain at yielding (%)	Rayleigh wave velocity (m s^{-1})
Polycarbonate	1400	65 ± 5	≈ 10	
Transparent epoxy	2830 ± 540	39 ± 1.2	1.4 ± 0.3	810–840

Table 1. The polycarbonate is the product of Lexan; it can sustain about 10% of extension without fracturing, and its tensile strength is 65 MPa. Axial extension was applied with an Instron 30 kN press at room temperature, atmospheric pressure and strain rates of $\dot{\epsilon} = 3.6 \times 10^{-5} \text{ s}^{-1}$ to $\dot{\epsilon} = 7 \times 10^{-3} \text{ s}^{-1}$. Continuous monitoring included axial displacement, axial load, broadband acoustic emission and video recording. The video recording enables a time resolution of 1/25 s (Reches et al., 2000). In a typical test, the fracturing started at 2–4% extension. Most tests were terminated when the polycarbonate layers yielded (by shear or tensile fracture), or when the epoxy layer delaminated from the polycarbonate.

The experimental work included six series of tests with up to 10 samples in each. Three types of matrix/hardener epoxy were used: (1) transparent, fast cementing epoxy, supplied by Chemibond, Israel. This epoxy contains many bubbles that apparently do not affect the fracture patterns; (2) dark, epoxy steel; and (3) bright, ‘rock cement’ glue by Makmolit. Tests with types (2) or (3) generated fracture patterns that are similar to those in published tests (Garrett and Baily, 1977; Rives et al., 1992; Wu and Pollard, 1995) and are not reported here.

4.2. Experimental observations

Eighteen samples with the transparent epoxy were tested. The tests differ from each other by the applied extension velocity; the velocity range is $0.5\text{--}60 \text{ mm min}^{-1}$ that corresponds to approximate strain rates of $\dot{\epsilon} = 3.6 \times 10^{-5} \text{ s}^{-1}$ to $\dot{\epsilon} = 7 \times 10^{-3} \text{ s}^{-1}$. The fracturing style of the epoxy depends strongly on the applied strain-rate (Table 2). Under strain rates slower than about 10^{-4} s^{-1} , the epoxy deformed continuously with only a few small fractures developing close to the grippers. These fractures are attributed to local gripping stresses. Strain rates higher than 10^{-4} s^{-1}

generate three different fracturing styles in the epoxy layer that we term: *planar*, *branching* and *clustering* (Table 2).

4.2.1. Planar fractures

Planar fractures developed under strain rates of $\approx 6 \times 10^{-4} \text{ s}^{-1}$. Some of the planar fractures crossed the complete width of the sample and they are composed of one or a few, en-échelon segments. Some of the planar fractures branched and formed simple fork structures; the branches either stopped within the sample or crossed the entire width. Branching is not common along these fractures and the maximum number of branches on a single fracture is five. Fracture spacing was measured along scan-lines in two samples; mean spacing is $4.8 \pm 1.1 \text{ mm}$ in A53, and irregular distribution in A54.

4.2.2. Branching fractures

Branching fractures developed under strain rates of $\approx 1 \times 10^{-3} \text{ s}^{-1}$. In test A56 almost all fractures were branched (Fig. 9a). A typical fracture here has a very short planar segment that splits into several branches in one or two branching junctions (Fig. 9b). The junctions may display a complex fork structure with three to six branches at a single junction. Branches form a structure with up to eight branching levels (Fig. 10). Fracture propagation directions were determined from branching directions, and it was found that most fractures initiated at the margins of the samples, whereas few initiated at the central part and propagated in two directions while branching (Fig. 9a).

The multiple branching increases the surface area and generates a structure with finite width of up to 7 mm. We measured the cumulative length of all branches associated with one branching fracture observed on the $\times 6.7$ magnification (Fig. 9b). This cumulative length was 178 mm; almost six times the length of a planar fracture across the

Table 2

Summary of experimental results

Fracturing style	Strain rate, $\epsilon \text{ (s}^{-1}\text{)}$	Fracturing style	Fracture density (FSR)
No fracturing	$< 10^{-4}$	Continuous flow without fracturing of the epoxy	NA
Planar	$\approx 10^{-4}$	Fractures are simple, planar and normal to extension axis; growth in few steps; some are shorter than sample width	≈ 0.2
Branching (Fig. 9a and b)	10^{-3}	Microbranches and few macrobranches; tree-like morphology; many macrobranches deviate in trend from parent fracture	0.25–2.5
Clustering (Fig. 9c–f)	$2 \times 10^{-3}\text{--}7 \times 10^{-3}$	<i>Clusters</i> : each with many tightly spaced, branched fractures that grew during a fast single event; new clusters may crosscut existing ones; very tight local spacing; local <i>fragmentation</i> of the brittle layer	10–13

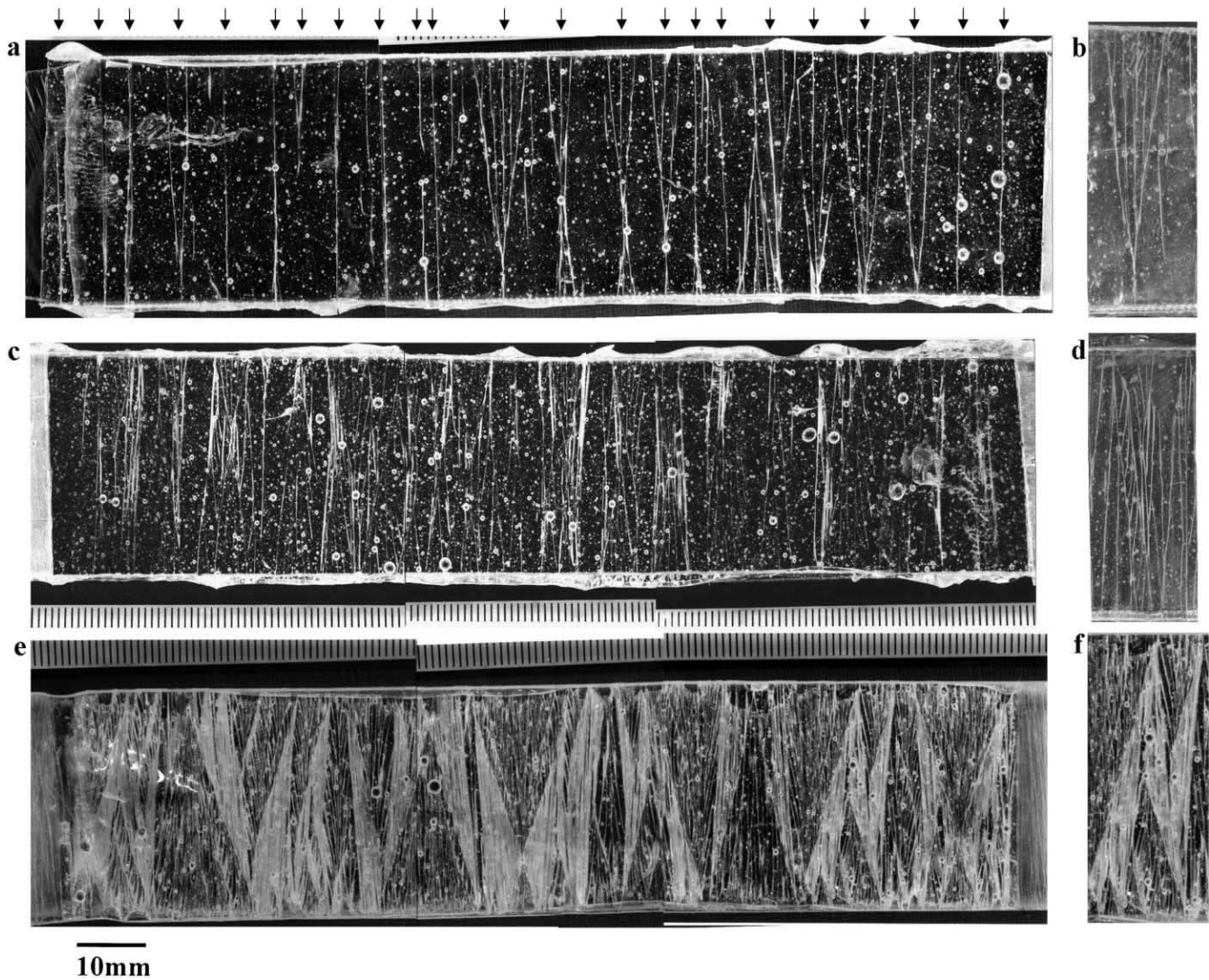


Fig. 9. Top view photographs of deformed, fractured samples; scale in mm; circular features are air bubbles in the epoxy. (a) and (b) Branching fractures in test A56. The fractures display a short planar segment that forks into several branches in simple to complex fork structures; each heavy arrow marked on the top indicates one branching fracture. (c) and (d) Clustering fractures in test A58; each cluster is a group of branching fractures that may be traced to its parent fracture. (e) and (f) Complex network of crosscutting clusters.

sample. The mean branching angle in this fracture was $16.3 \pm 8.5^\circ$, and most branches maintain their branching orientation through their entire length. Therefore, the fracture segments within a branching fracture may show a 'conjugate set' on which the fractures significantly deviate from the expected tension-normal direction.

Two types of fracture spacing were measured in the A56 test: (1) the spacing between the 23 main branching fractures marked by tick arrows in Fig. 9a. This measurement yielded mean spacing of 5.0 ± 1.8 mm for 23 fractures that are 1.5 mm long or more; and (2) the spacing of all branches along a scan-line. This measurement yielded mean spacing of 2.3 ± 1.9 mm.

4.2.3. Clustering fractures

Five tests were run under high strain rates of $2 \times 10^{-3} \text{ s}^{-1}$

to $7 \times 10^{-3} \text{ s}^{-1}$. These tests yielded a fracturing style that we term 'clustering'; this style is reported here for the first time in layered media under quasi-static loading. A 'clustering fracture' is a group of branching fractures that crosscut each other and form a wide zone of intense fracturing within the brittle layer. In the simple clusters, each branch may be traced to its main fracture (Fig. 9c and d). In the more complex clusters, however, this tracing is impossible and the 'clustering fracture' is regarded as one structural unit (Fig. 9e and f).

The experiments indicate that a clustering fracture grows during a single and fast event (Reches et al., 2000). This is demonstrated in Fig. 11 that displays sequences of consecutive frames from the video records of test A58; the time span between two consecutive frames is 0.04 s. Clustering fractures appear here as dark structures on the gray

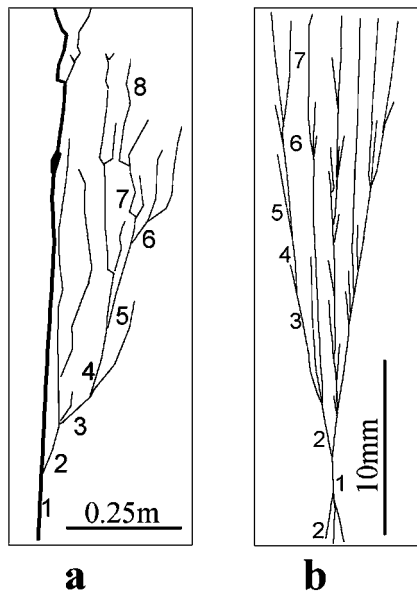


Fig. 10. Multilevel branching in the dolomite layer of Arugot (a) and in test A56 (b); numbers indicate branching level.

background of the sample. This figure clearly shows that a cluster was fully developed during the time of a single frame: cluster A developed in frame #2, cluster B developed in frame #5 and cluster C developed in frame #7 (Fig. 11). The fully developed cluster may continue to dilate after the initial growth, for example, cluster B dilates from frame #6 to #7.

The general trend of the clusters is normal to the extension axis; however, the individual branches deviate significantly from the general trend. The mean branching angle for a single cluster in test A58 was $16.8 \pm 6.7^\circ$, which is the same as the $16.3 \pm 8.5^\circ$ angle in test A56 of $\dot{\epsilon} = 1 \times 10^{-3} \text{ s}^{-1}$ (see above).

The intense fracturing within the cluster generated a fragmentation zone in the brittle layer. The cumulative length of the fracture segments inside a single cluster was measured under a $6.7\times$ magnification. The measured length is 505 mm, which is 17 times the length of a planar fracture across the sample. The average spacing between the central-lines of the clusters in sample A56 was 7.3 ± 2.2 mm. The fracture density increased profoundly in tests of $\dot{\epsilon} \approx 7 \times 10^{-3} \text{ s}^{-1}$ in which $\text{FSR} \approx 10$ for the entire sample and locally $\text{FSR} \approx 13$. This high fracture density reflects another new feature of clustering fractures: they crosscut and partly overlap each other (Figs. 9d and 12). This style is in clear contrast to previous experiments in which tensile fractures did not cross each other and did not form close to existing ones (Garrett and Baily, 1977; Rives et al., 1992; Wu and Pollard, 1995). The present experiments show that the development of clustering fractures is an efficient mechanism to fragment the brittle layer under quasi-static loading.

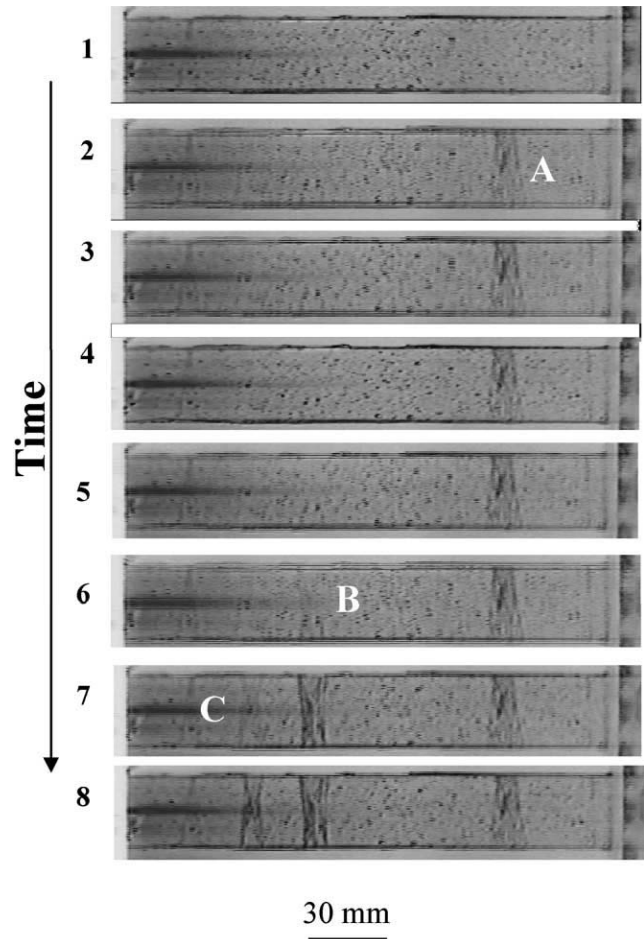


Fig. 11. Growth of fracture clusters displayed by snapshots in test A58. For continuous video display in real time see Reches et al. (2000). Clusters appear by dark structures on the gray background of the sample; time progress is from frames 1 to 4 that are consecutive snapshots with 1/25 s between each pair; snapshots 5 to 8 are also consecutive frames on the video records. A, B and C indicate stages of cluster appearance and dilation (see text).

4.3. Microbranching

The branches described above depart from the parent fracture at an angle of $\approx 16^\circ$, and they propagated to a distance of a few millimeters (or more) without changing their orientations. These features are similar to macrobranches observed in fracturing tests of brittle plates (Fig. 1a) (Schardin, 1959; Ramulu and Kobayashi, 1985). Another type of branch, termed 'microbranches', appeared in the present experiments. The microbranches are short, up to 100 μm long, they depart from the parent fracture at an angle of $\approx 30^\circ$ and they curve to gradually parallel to the parent fracture (Fig. 13a). The microbranch geometry fits the form of $y \propto ax^b$ (Fig. 13b), where x is the distance along the parent fracture, y is the distance normal to it, and a and b are constants. The measured microbranches have $b \approx 0.77 \pm 0.01$, and a ranges from 0.07 to 0.76. The

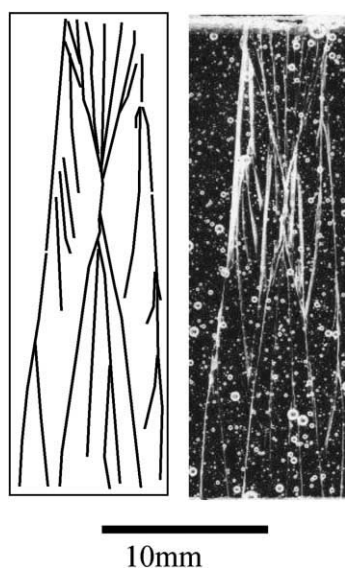


Fig. 12. Close-up of a simple cluster with three (and more) branching fractures that formed simultaneously. Photograph (right) and fracture tracing (left); note slight curving of some branches that suggest interaction between the fractures.

geometry of the microbranches in the epoxy layers is similar to the microbranches observed along dynamic fractures in glass and PMMA (Sharon and Fineberg, 1999) (Fig. 13c). Further, the determined b value is essentially identical to the $b = 0.70$ found by Sharon and Fineberg (1996).

4.4. Propagation velocity of the epoxy fractures

One of the objectives was to determine the velocity of fracture propagation in the epoxy layers. Our attempts were successful only for the slow propagating fractures that could be traced on the video records (Reches et al., 2000). However, the velocity of the fast growing fractures exceeded the available techniques and we could only estimate a lower bound on this velocity. From Fig. 11, which displays sequences of consecutive frames from test A58, we estimated a minimum fracture velocity to cross the 30 mm of sample width within one video frame of 0.04 s as 0.75 m s^{-1} .

Alternatively, several morphological features of the fractures in the present experiments suggest higher propagation velocities for most fractures in tests of $\dot{\epsilon} \geq 1 \times 10^{-3} \text{ s}^{-1}$. First, previous tensile experiments of brittle plates show that micro- and macrobranches develop only along dynamic fractures (Ramulu and Kobayashi, 1985; Lawn, 1993; Sharon and Fineberg, 1996). Similarly, the fractures in the present experiments display intense branching and microbranching in tests subjected to strain rates of $1\text{--}7 \times 10^{-3} \text{ s}^{-1}$ (see above). Second, the geometry of the microbranches in the epoxy is essentially identical to that in the glass and PMMA (Fig. 13b and c). The Rayleigh wave velocity of the epoxy used here is $810\text{--}840 \text{ m s}^{-1}$ (kindly measured by E. Sharon, 1999). Using the $V_c \approx 0.4V_R$ as the

critical velocity needed for microbranch development (Sharon and Fineberg, 1996), the minimum value for the propagation velocity of the clustering fractures is about 325 m s^{-1} .

5. Discussion

5.1. Propagation velocity of the tree-like joints in Arugot

It is proposed here that the tree-like joints in the Arugot outcrop propagated at dynamic velocities. This deduction is based on two central observations. First, the tree-like joints mapped in the field are similar in morphology to dynamic fractures observed in experiments (Table 3). The striking similarities include multiple branching (up to nine orders in Fig. 10), common occurrence of a main fracture with many secondary ones (Fig. 14), tendency of many branches to parallel the main fracture (Figs. 1b and 3), and the general shape, which is similar over two orders of magnitudes in dimensions (Figs. 10 and 14). We also note the dissimilarity of macrobranching angles that are $\approx 45^\circ$ in the dolomite and $\approx 16^\circ$ in the epoxy tests.

The second observation is the profound increase of the surface area. Our field measurements revealed that the surface area of a tree-like joint is 9–14 times the surface area of a smooth one; this is a conservative estimate as it is based on mapping at a scale of 1:1, and surface area increase at microscopic scale is not accounted. Similar intensity of surface area increase was observed in experimental dynamic fractures. In the present work, the dynamic fractures in the epoxy layers display 6–17 times increase in surface area with respect to a planar fracture (Figs. 9 and 10b). Also, the cumulative surface area of a fracture that grows at the terminal velocity, $V_T \approx 0.7V_R$, is six times the surface area of a planar fracture (Sharon and Fineberg, 1996). These authors showed that the increase of surface area prevents fractures from reaching the theoretical velocity V_R , because “...the system ‘chooses’ not to dissipate the excess energy... by increasing the crack velocity, but to divert the energy into the creation of additional surface area”. It is postulated here that the surface area increase associated with tree-like joints indicates dynamic propagation velocities similarly to glass and PMMA.

To estimate the propagation velocity of the dynamic joints in Arugot, we use the clear experimental observation that micro- and macrobranches and the profound increase of surface area are associated only with fractures that propagate at velocities above 40% of Rayleigh wave velocity (see Section 2). As discussed above, branching and surface area increase are intrinsic features of dynamic fracturing. Thus, based on the tree-like morphology and surface area increase (Table 3), one can deduce that the growth velocity of Arugot joints was significantly larger than the critical velocity (also Sharon, personal communication, 1999). The mean Rayleigh wave velocity for dolomites is $V_R \approx 2750 \text{ m s}^{-1}$

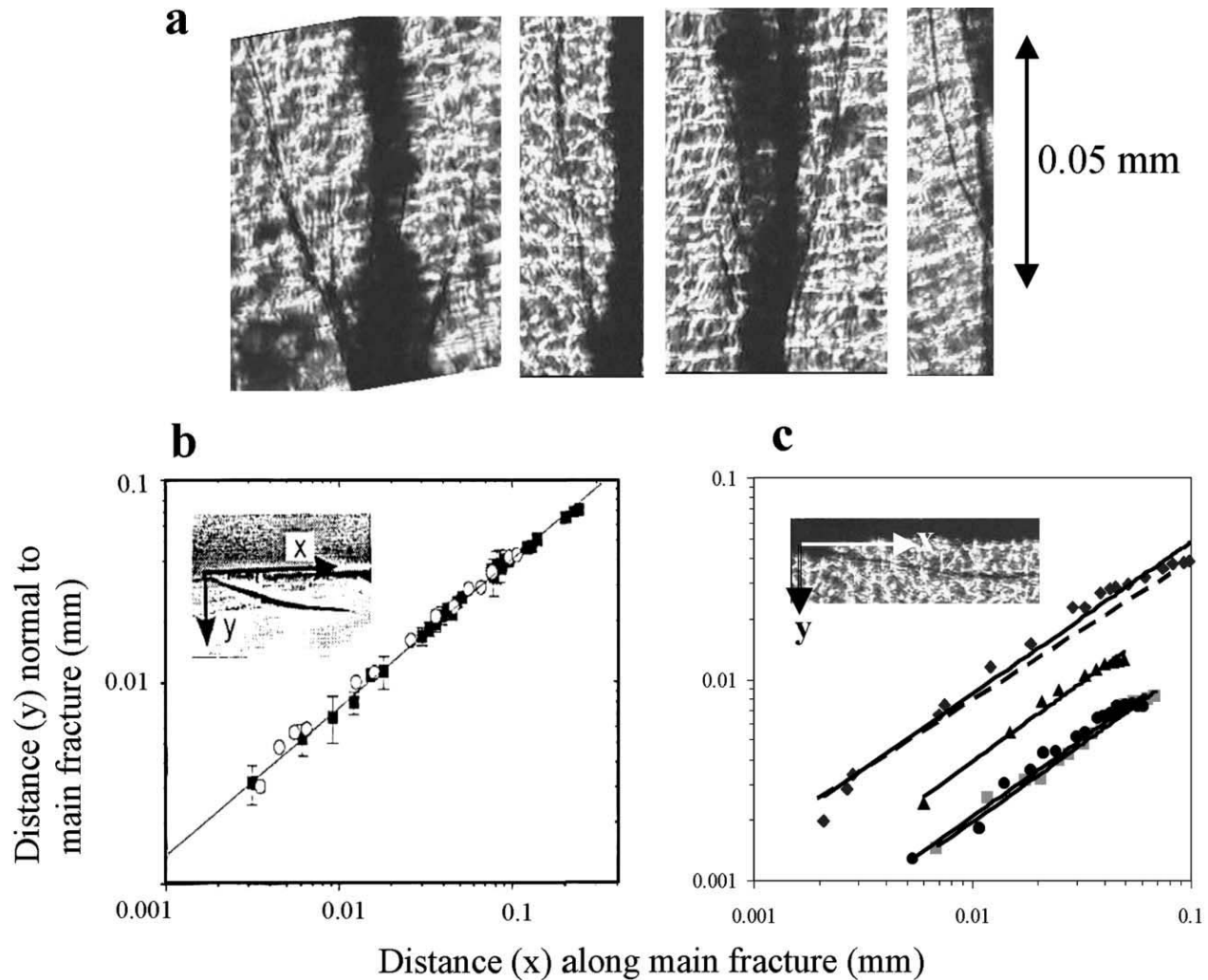


Fig. 13. Microbranches along dynamic fractures. (a) Microbranches along fractures in the epoxy layers of present experiments: thin, dark, curved lines that branch upward from the main, thick fracture. (b) Geometry of microbranches in plates of glass (open circle) and PMMA (solid squares); after Sharon and Fineberg (1999). (c) Geometry of microbranches in the epoxy layers measured by digitizing along the microbranches; each symbol refers to a different microbranch; thin line indicates best fit power-law curve; in (b) and (c), the main fracture propagated horizontally from left to right (positive x) and branching direction is to the right and downward (see inserts); note similarity of slopes in (b) and (c) (see text).

(Mavko et al., 1998), therefore the estimated propagation velocity for Arugot joints is $V > V_C \approx 1100 \text{ m s}^{-1}$.

This inference that Arugot joints propagated dynamically raises two important questions. The first is related to the propagation direction of dynamic fractures in layered media. Experiments on dynamic fracturing were conducted with 2D single, unconfined plates (Fig. 1) (Schardin, 1959; Ravi-Chandar and Knauss, 1982; Sharon and Fineberg, 1996), or with layered media of a thin brittle layer between thicker, ductile ones (present experiments, Fig. 8). The dynamic fractures in these experiments propagated primarily parallel to the plate (or layer) surfaces. The dominant propagation direction in the Arugot outcrop is apparently different: it is normal to the surface of the dolomite layer, as evident by the branching direction observed on the sub-vertical outcrop wall (Fig. 3). Due to limited field exposure of this joint set, one cannot observe evidence for (or against)

layer-parallel propagation (Fig. 2c). Our above deduction that Arugot joints propagated at dynamic velocities was based on observations of surface area, intense branching and high joint density; these features are not related to bedding surfaces or layer-parallel anisotropy. Therefore, we think that the apparent difference in the relative propagation direction between field and experiments should not change the main results.

The second question is related to the rate of loading associated with Arugot dynamic joints. There are few cases of fracturing that clearly indicate high loading rates, for example, shatter cones that are associated with meteorite impacts, or fragmentation and pulverization under explosive condition (Grady and Kipp, 1987). However, branching fractures in brittle plates look similar for different loading rates (Schardin, 1959; Sharon and Fineberg, 1996). Therefore, in general, one cannot discriminate between dynamic

Table 3
Comparing morphological features of dynamic fractures

	Tree-like joints in the field (present work)	Fractures in layered composites (present work)	Fractures in brittle plates ^a
Macrobranching	Branching up to nine orders; branching angle $\approx 45^\circ$; curving to parallel main fracture (Figs. 3–5)	Branching up to eight orders; branching angle $\approx 16^\circ$ (Figs. 9 and 10)	Branching in several orders (Fig. 1a)
Microbranching		Up to 100 μm long, curved shape of the relations $\gamma\alpha x^{0.78}$ (Fig. 13)	Up to 100 μm long, curved shape of the relations $\gamma\alpha x^{0.7}$, appear above critical velocity (Figs. 1b and 13)
Fracture density	Very high density (FSR > 22.0) (Figs. 6 and 7)	High density (local values FSR ≈ 13) (Fig. 9e and f)	
Surface area	9–14 times the area of a smooth fracture	Significant increase	Six times the area of a smooth fracture
Propagation velocity	Deduced to be dynamic, thus, $V > V_C \approx 0.4V_R \Rightarrow$ $V > 1100 \text{ m s}^{-1b}$	Deduced to be dynamic thus, $V > V_C \approx 0.4V_R$ (epoxy), \Rightarrow $V > 325 \text{ m s}^{-1}$	Dynamic velocity: $V > 0.4V_R$ with short stages of $V \rightarrow V_R$

^a After: Ramulu and Kobayashi (1985); Bahat (1991); Sharon and Fineberg (1996).

^b Velocity calculations after Mavko et al. (1998).

fractures that develop under high loading rates and those which develop under quasi-static loading. It is likely that the dolomite layers in Arugot were subjected to quasi-static extension, which is typical for geological processes. However, the immediate proximity of the studied exposure

to a large normal fault (Fig. 2b) suggests that high loading rates associated with earthquakes could also be important to the dynamic nature of the fracturing.

5.2. Fracture clustering: a new fracturing style

To the best of our knowledge, the present experiments are the first report of dynamic fracturing in a layered sequence of brittle and ductile layers. In addition to known forms of planar fractures and branching fractures (Fig. 9a and b), the experiments revealed a new style of fracturing that is termed here *fracture clustering* (Section 4.2.3 and related figures; Reches et al., 2000). Fracture clustering is most likely controlled by the layered nature of the samples; however, at the present stage of the research, the exact mechanism of this process is unknown.

The unique features of this style are:

1. Simultaneous development of many, closely spaced tensile fractures with branching geometry (Fig. 11; Reches et al., 2000);
2. Development of ‘pseudo conjugate set’ of tensile fractures (Figs. 9f and 12);
3. Crosscutting relations between close fractures inside a cluster.

While fracture clustering has not been recognized as fracturing style, some previous studies displayed features that resemble the present results. Roman et al. (1992) extended a brittle carbon rod embedded in titanium alloy, and they found clusters of fractures in the brittle rod. Each cluster is composed of 2–5 fractures and some of them display a branching shape (Fig. 15) while the spacing between the clusters was large, about 1–2 times the rod diameter. The

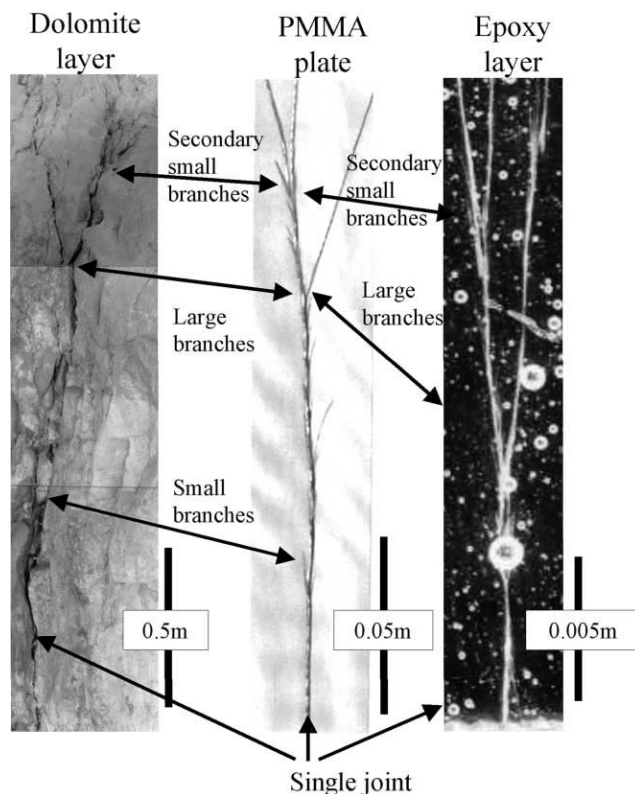


Fig. 14. Morphological similarity of macrobranches in dolomite (left), PMMA plate (center) and epoxy (right); note scale differences. E. Sharon kindly provided the PMMA sample.

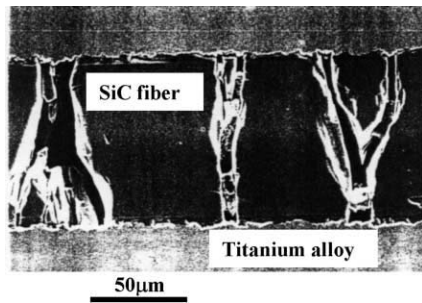


Fig. 15. Tensile fractures within a brittle SiC fiber embedded in titanium alloy matrix (after Roman et al. (1992)); note complex branching in the three groups of fractures.

present experiments suggest that the clusters in Fig. 15 could form as dynamic fractures.

5.3. Fracture clustering and high density of joints

High joint density was found in the Arugot exposure, $FSR > 20.0$ in the proximity of a normal fault (Fig. 7). The compilation of some previous field observations (Fig. 16) displays two distinct groups of fracture density. Group A with low FSR values of 0.5–3.0 that includes many field outcrops with joint density of $FSR \approx 1.0$ (Narr and Suppe, 1991; Gross, 1993) and Group B with high FSR values of 1.0–22.0; the present results clearly belong to this group.

The density of opening mode fractures in layered media was studied in several experimental works (Garrett and Baily, 1977; Rives et al., 1992; Wu and Pollard, 1995).

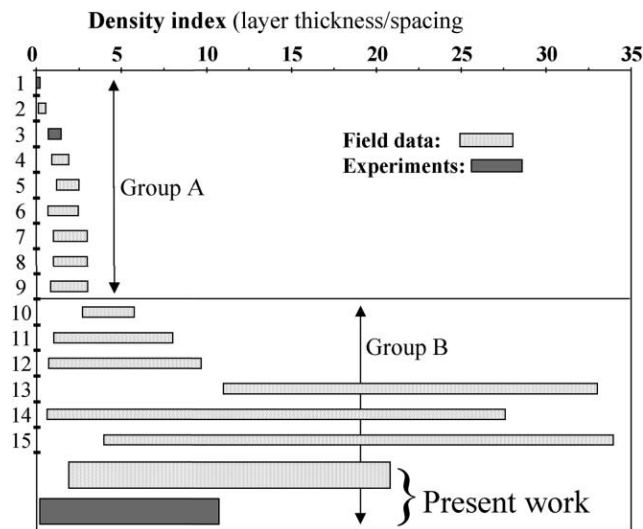


Fig. 16. Compilation of joint (and fracture) density in the field and in experiments; each rectangle shows the minimum (left) and maximum (right) values of FSR measured in the published data; lowest two rectangles are for the present work. Sources are the following: 1 and 4: Wu and Pollard (1995); 2 and 5: Narr and Suppe (1991); 3: Garrett and Baily (1977); 6: Gross (1993); 7: Huang and Angelier (1989); 8: Price (1966); 9: Gross et al. (1995); 10: Rives et al. (1992); 11: McQuillan (1973); 12: Becker and Gross (1996); 13: Reches (1998); 14: Reches (1972); 15: Ladeira and Price (1981).

The tested layered samples were subjected to layer-parallel extension and, typically, one set of fractures developed in the brittle layer normal to the direction of extension. Fracture density increased with increasing extension up to a stage termed ‘fracture saturation’ (Narr and Suppe, 1991; Rives et al., 1992; Wu and Pollard, 1995). During this stage, new fractures cease to develop, existing fractures dilate, and eventually the ductile layers fail (Wu and Pollard, 1995) or delaminate from the brittle layers (Roman et al., 1992). The fracture density during saturation reaches a maximum value of $FSR \approx 1.0$ (Garrett and Baily, 1977; Rives et al., 1992; Wu and Pollard, 1995) (Fig. 16).

Theoretical models of joint density in brittle/ductile layered composites are usually based on the assumption that an existing joint creates a ‘stress shadow’ due to a drop in the tensile stresses at its proximity (Price 1966; Hobbs, 1967; Sowers, 1973; Gross et al., 1995; Ji et al., 1998; Bai and Pollard, 2000). The tensile stress rises gradually with distance from the joint, until it exceeds rock strength and a new joint forms. Some of these models predict an upper limit on the density values, $FSR \leq 1.0$, that is attributed to the stress shadow and the finite strength (or finite modulus) of the ductile layers. Thus, the high density of joints (Group B in Fig. 16) contradicts the stress shadow concept. Other mechanisms were proposed to explain the high-density observations. For example, Ladeira and Price (1981) proposed repeated hydraulic fracturing, and Becker and Gross (1996) suggested local strain increase.

The present experimental results of dynamic fracturing in layered media raise a new mechanism for high fracture density. The clusters of fractures observed in the present experiments display very high density of tensile, branching fractures in the brittle layer (Fig. 9e and f). The cumulative length of fractures in the cluster indicates density values of $FSR > 10.0$. Each cluster grows during a single dynamic event and, initially, the clusters are widely spaced (Figs. 11 and 17a) (Reches et al., 2000). As the extension increases, new clusters fill the unfractured regions (Fig. 17b) and, eventually, clustering stops when a final spacing S_f between the clusters is attained (Fig. 17c). In the present experiments, S_f between branching and clustering fractures is similar to S_f between planar fractures (Fig. 17d). However, the surface area of the fractures within the clusters is very high; for example, in a strain rate of $1 \times 10^{-3} \text{ s}^{-1}$, the cumulative fracture length is six times larger than the length of a planar fracture formed under strain rate of $6 \times 10^{-4} \text{ s}^{-1}$. At strain rates of 2×10^{-3} – 7×10^{-3} , the fracture length within a single cluster is 17 times the length of a planar fracture. It is apparent that the final high density of dynamic fractures within a layered medium reflects two independent factors: the internal cumulative surface area of a single complex fracture or cluster ($FSR > 10.0$), and the wide spacing between the individual complex fractures ($FSR < 1.0$).

Using the above concept, we suggest that the high joint density measured in Arugot reflects the increased surface

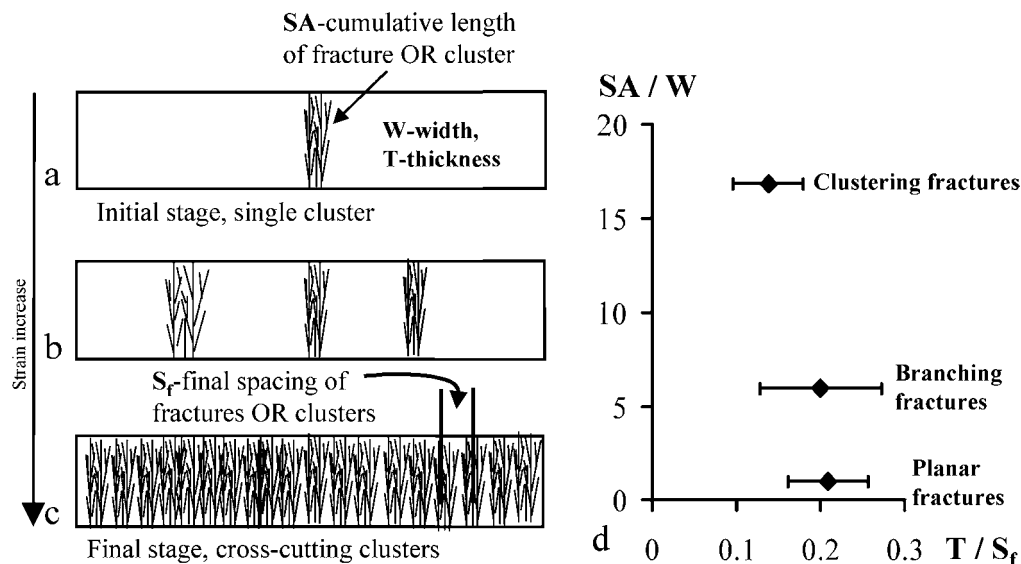


Fig. 17. Development of high fracture density by dynamic fracturing in a layered medium. (a) The first cluster forms with SA cumulative fracture length inside the cluster (see text); (b) and (c) Extension increase and new clusters fill the unfractured regions with final spacing S_f between clusters ($FSR < 1.0$). Final density of the dynamic fractures is composed by intra-cluster density of a single cluster (SA/W), and the sum of all clusters. (d) Relations between intra-cluster density and density of individual clusters ($FSR = T/S_f$) in three experiments (A53, A56 and A58).

area of tree-like joints and clusters during dynamic fracturing. The gradual increase of density toward the fault probably indicates a gradual strain increase along the layer and toward the fault. Finally, the observed fragmentation reflects overlapping of clustering and branching fractures, a phenomenon observed in our experiments (Fig. 9e) and recognized in the field (Fig. 6).

6. Conclusions

The present work indicates that dynamic propagation velocity can be recognized by the tree-like morphology of individual joints in the field and by their tight spacing. These two criteria allow the recognition of fast fracturing during past catastrophic events. These criteria could eventually provide a solution for a long-standing enigma of recognizing paleoseismic events by the morphology of a fault zone and its associated fractures.

A new class of fractures, the clustering fractures, are analyzed here for the first time. This class of fracturing in brittle/ductile composites is an effective mechanism for generating closely spaced joints in the field and experiments.

Acknowledgements

Discussions with Jay Fineberg, Eran Sharon, Leonid Germanovich and Dov Bahat are greatly appreciated. The careful reviews of Terry Engelder and Michael Gross significantly contributed to the quality of the manuscript. Thanks to Rod Holcombe for the permit to use the GeOrient program. The study was supported by “The Alexander

Silberman Hebrew Univ. Foundation for Applied Science”, “Minerva Dead Sea Research Center, Tel-Aviv Univ.” and the “US-Israel Binational Science Foundation”.

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